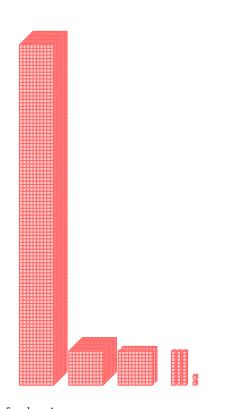
WHOLE NUMBERS

A BUILDING NUMBERS

A.1 COUNTING CUBES IN A TABLE

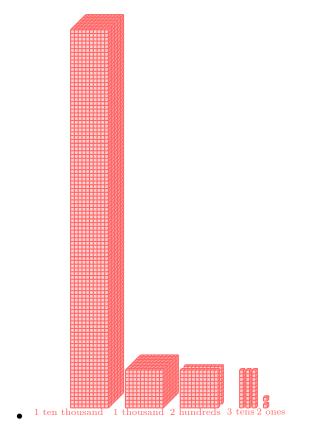
Ex 1:



The number of cubes is

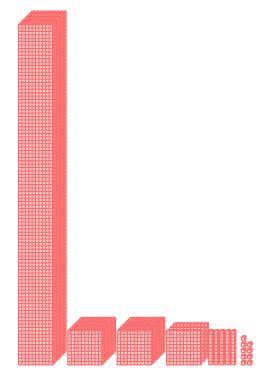
Ten thousands	Thousands	Hundreds	Tens	Ones
1	1	2	3	2

Answer:



	Ten thousands	Thousands	Hundreds	Tens	Ones
•	1	1	2	3	2

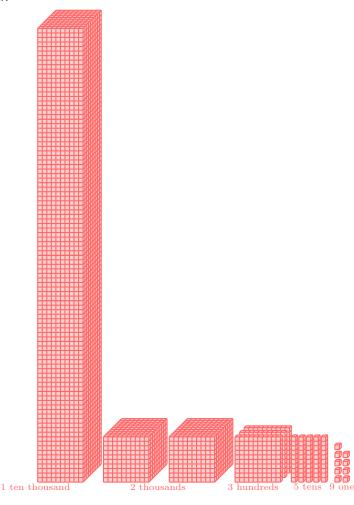
Ex 2:



The number of cubes is

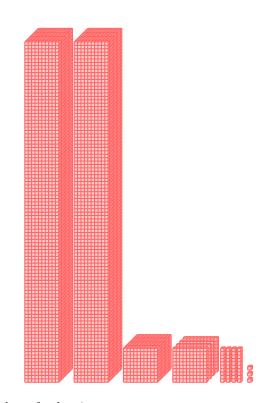
Ten thousands	Thousands	Hundreds	Tens	Ones
1	2	3	5	9

Answer:



Ten thousands	Thousands	Hundreds	Tens	Ones
1	2	3	5	9

Ex 3:

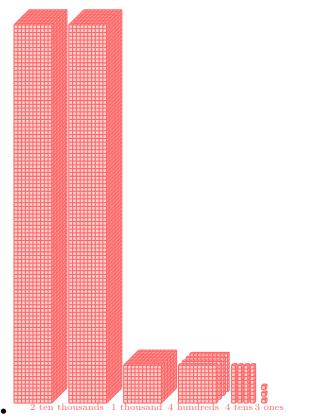


The number of cubes is

Ten thousands	Thousands	Hundreds	Tens	Ones
2	1	4	4	3

Answer:

Ex 4:

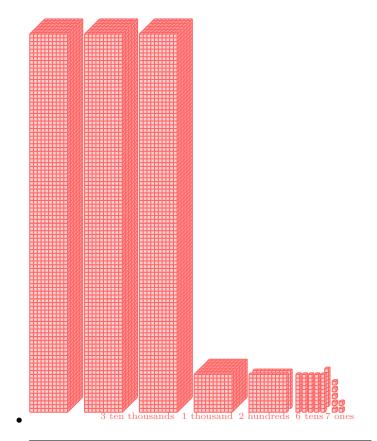


Ten thousands	Thousands	Hundreds	Tens	Ones
2	1	4	4	3

The number of cubes is

Ten thousands	Thousands	Hundreds	Tens	Ones
3	1	2	6	7

Answer:



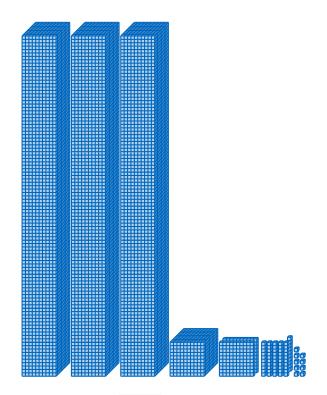
	Ten thousands	Thousands	Hundreds	Tens	Ones
•	3	1	2	6	7

A.2 COUNTING CUBES

Ex 5:

2





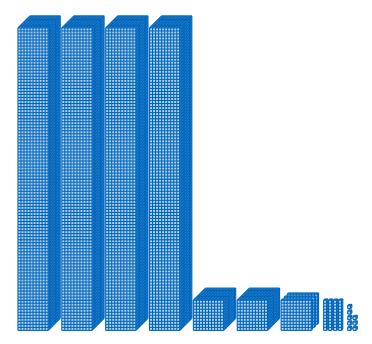
The number of cubes is 31269

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	3	1	2	6	9

• The number of cubes is 31 269.

Ex 6:



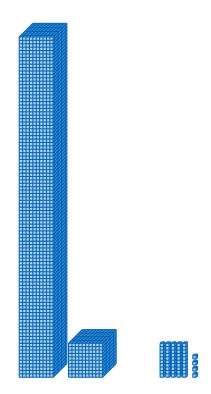
The number of cubes is $\boxed{42348}$.

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	4	2	3	4	8

• The number of cubes is 42 348.

Ex 7:



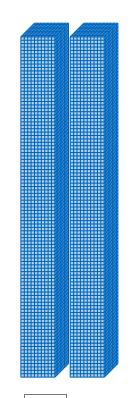
The number of cubes is 11054

Answer:

_	Ten thousands	Thousands	Hundreds	Tens	Ones
•	1	1	0	5	4

• The number of cubes is 11054.

Ex 8:



The number of cubes is 20000.

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	2	0	0	0	0

• The number of cubes is 20 000.

A.3 COUNTING CUBES FROM A TABLE

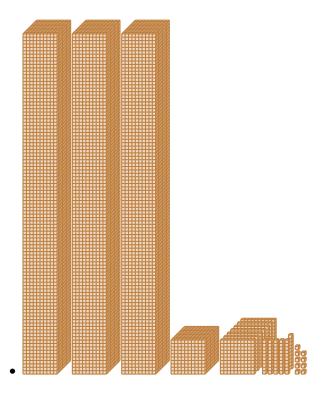
Ex 9:

Ten thousands	Thousands	Hundreds	Tens	Ones
3	1	7	6	9

The number is $\boxed{31769}$.

Answer:

• 3 ten thousands + 1 thousand + 7 hundreds + 6 tens + 9 ones.



- $30\,000 + 1\,000 + 700 + 60 + 9$
- The number is 31 769.

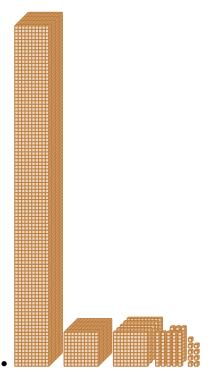
Ex 10:

Ten thousands	Thousands	Hundreds	Tens	Ones
1	1	5	8	9

The number is 11589.

Answer:

ullet 1 ten thousands + 1 thousand + 5 hundreds + 8 tens + 9 ones.



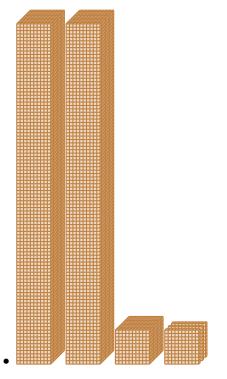
- $10\,000 + 1\,000 + 500 + 80 + 9$
- \bullet The number is 11 589.

Ex 11:

(D) (1 1	/D1 1	TT 1 1	m	
Ten thousands	1 nousands	Hunareas	rens	Ones
2	1	3	0	0

The number is $\boxed{21300}$.

Answer:



- 20000 + 1000 + 300 + 0 + 0
- The number is 21 300.

A.4 FINDING THE DIGIT

Ex 12: The digit in the hundreds place of 24 325 is 3.

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	2	4	3	2	5

• The digit in the hundreds place of 24325 is 3.

Ex 13: The digit in the ten thousands place of 41 092 is 4.

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	4	1	0	9	2

• The digit in the ten thousands place of 41 092 is 4.

Ex 14: The digit in the ones place of 4109 is 9.

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	0	4	1	0	9

• The digit in the ones place of 4109 is 9.

Ex 15: The digit in the tens place of 31 267 is 6

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	3	1	2	6	7

• The digit in the tens place of 31 267 is 6.

Ex 16: The digit in the thousands place of 21 443 is 1.

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	2	1	4	4	3

• The digit in the thousands place of 21 443 is 1.

A.5 WRITING NUMBERS FROM TEN THOUSANDS, THOUSANDS, HUNDREDS, TENS, AND ONES

Ex 17: 3 ten thousands + 2 thousands + 3 hundreds + 2 tens + 8 ones $= \boxed{32328}$

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	3	2	3	2	8

• 3 ten thousands + 2 thousands + 3 hundreds + 2 tens + 8 ones = 32 328

Ex 18: 4 ten thousands + 5 thousands + 1 hundred + 9 tens + 6 ones $= \boxed{45196}$

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	4	5	1	9	6

 \bullet 4 ten thousands + 5 thousands + 1 hundred + 9 tens + 6 ones = $45\,196$

Ex 19: 6 ten thousands + 1 thousand + 5 hundreds + 2 tens + 9 ones = 61529

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	6	1	5	2	9

ullet 6 ten thousands + 1 thousand + 5 hundreds + 2 tens + 9 ones $=61\,529$

Ex 20: 2 ten thousands + 7 hundreds + 4 tens + 3 ones = 20743

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	2	0	7	4	3

 \bullet 2 ten thousands + 0 thousands + 7 hundreds + 4 tens + 3 ones = $20\,743$

A.6 WRITING NUMBERS FROM EXPANDED FORM

Ex 21: $30\,000 + 2\,000 + 300 + 20 + 8 = \boxed{32328}$

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	3	2	3	2	8

• $30\,000 + 2\,000 + 300 + 20 + 8 = 32\,328$

Ex 22: $40\,000 + 5\,000 + 100 + 90 + 6 = \boxed{45196}$

Answer.

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	4	5	1	9	6

• $40\,000 + 5\,000 + 100 + 90 + 6 = 45\,196$

Ex 23: $20\,000 + 700 + 40 + 3 = \boxed{20743}$

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	2	0	7	4	3

 $\bullet \ 20\,000 + 700 + 40 + 3 = 20\,743$

Ex 24: $60\,000 + 1\,000 + 500 + 20 + 9 = \boxed{61529}$

Answer:

Ten thousands	Thousands	Hundreds	Tens	Ones
6	1	5	2	9

 $\bullet \ 60\,000 + 1\,000 + 500 + 20 + 9 = 61\,529$

A.7 WRITING NUMBERS FROM EXPANDED FORM

Ex 25: $6 \times 10\,000 + 2 \times 1\,000 + 5 \times 100 + 2 \times 10 + 9 \times 1 = \boxed{62529}$

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	6	2	5	2	9

•
$$6 \times 10000 + 2 \times 1000 + 5 \times 100 + 2 \times 10 + 9 \times 1 = 62529$$

Ex 26: $4 \times 10\,000 + 3 \times 1\,000 + 7 \times 100 + 1 \times 10 + 6 \times 1 = \boxed{43716}$

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	4	3	7	1	6

•
$$4 \times 10\,000 + 3 \times 1\,000 + 7 \times 100 + 1 \times 10 + 6 \times 1 = 43\,716$$

Ex 27: $1 \times 10\,000 + 2 \times 1\,000 + 8 \times 100 + 5 \times 10 + 0 \times 1 = \boxed{12850}$

Answer:

	Ten thousands	Thousands	Hundreds	Tens	Ones
•	1	2	8	5	0

•
$$1 \times 10000 + 2 \times 1000 + 8 \times 100 + 5 \times 10 + 0 \times 1 = 12850$$

Ex 28: $5 \times 10\,000 + 9 \times 1\,000 + 0 \times 100 + 3 \times 10 + 7 \times 1 = \boxed{59037}$

Answer:

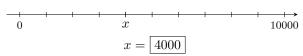
	Ten thousands	Thousands	Hundreds	Tens	Ones
•	5	9	0	3	7

• $5 \times 10\,000 + 9 \times 1\,000 + 0 \times 100 + 3 \times 10 + 7 \times 1 = 59\,037$

B ON THE NUMBER LINE

B.1 FINDING NUMBERS

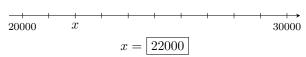
Ex 29:



Answer:



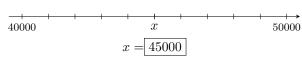
Ex 30:



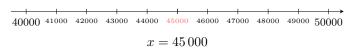
Answer:



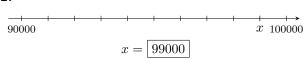
Ex 31:



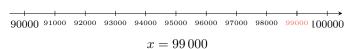
Answer:



Ex 32:



Answer:



C BIG NUMBERS

C.1 COUNTING FROM A TABLE

Ex 33:

billions H T U			millions			thousands			units		
Н	Т	U	Н	Т	U	Н	Т	U	Η	Т	U
0	0	0	0	0	1	2	5	0	0	0	0

The number is $\boxed{1250000}$

Answer: The number is 1250000.

Ex 34:

b	illior	ıs	millions			thousands			units		
Н	Т	U	Н	Т	U	Н	Т	U	Н	Т	U
0	0	0	0	1	2	0	0	0	0	0	0

The number is 12000000.

Answer: The number is 12 000 000.

Ex 35:

b	illior	lions	S	millions			tho	ousar	nds	units			
Н	Т	T	U	Н	Т	U	Н	Т	U	Н	Т	U	
0	H T U		0	1	3	5	0	0	0	0	0	0	

The number is 135000000

Answer: The number is 135 000 000.

Ex 36:

b	illion	ıs	m	millions			thousands			units		
Н	Т	U	Н	Т	U	H T U			Η	Т	U	
3	H T U 3 4 0		1	1 2 0			0	0	0	0	0	

The number is 340120000000

Answer: The number is 340 120 000 000.

C.2 WRITING NUMBERS FROM WORDS

Ex 37: One million two hundred fifty thousand is 1250000

Answer:

• One million two hundred fifty thousand is:

b	illion	ıs	millions			tho	ousar	$_{ m nds}$		units	;
Н	Т	U	Н	H T U			Т	U	Н	Т	U
0	0	0	0	0	1	2	5	0	0	0	0

• One million two hundred fifty thousand is 1 250 000.

Ex 38: Twenty-five million four hundred thousand is 25400000

Answer:

• Twenty-five million four hundred thousand is:

b	illior	ıs	m	illio	ns	tho	ousai	$_{ m nds}$	unit H T		ts	
Н	Т	U	Н	Т	U	Н	Т	U	Н	Т	U	
0	0	0	0	2	5	4	0	0	0	0	0	

• Twenty-five million four hundred thousand is 25 400 000.

Ex 39: One hundred ninety million is 190000000

Answer:

• One hundred ninety million is:

b	illior	ıs	millions			tho	ousar	$_{ m nds}$		units	3
Н	Т	U	Н	H T U			Т	U	Н	Т	U
0	0	0	1	9	0	0	0	0	0	0	0

• One hundred ninety million is 190 000 000.

Ex 40: Twenty-one billion seven hundred million is 21700000000.

Answer:

• Twenty-one billion seven hundred million is:

b	illior	ıs	m	millions		the	ousai	$_{ m nds}$		units	3
Н	Т	U	Н	H T U			Т	U	Н	Т	U
0	2	1	7	0	0	0	0	0	0	0	0

• Twenty-one billion seven hundred million is 21 700 000 000.

C.3 COUNTING IN REAL-WORLD PROBLEMS

Ex 41: The Jurassic era was about one hundred and fifty million years ago. Write this number in positional notation:

| 150000000 | years ago

Answer:

• One hundred fifty million is:

b	illior	ıs	millions			tho	ousai	$_{ m nds}$		units	3
Η	Т	U	Н	Т	U	Н	Т	U	Н	Т	U
0	0	0	1	5	0	0	0	0	0	0	0

 \bullet One hundred fifty million is $150\,000\,000$ years ago.

Ex 42: The estimated global population in 2020 was about seven billion eight hundred million people. Write this number in positional notation:

7800000000 people

Answer:

• Seven billion eight hundred million is:

b	illior	ıs	m	millions			ousai	ds	1	units	5
Η	Т	U	Η	H T U			Т	U	Н	Т	U
0	0	7	8	0	0	0	0	0	0	0	0

• Seven billion eight hundred million people is 7 800 000 000 people.

Ex 43: Astronomers estimate that our galaxy, the Milky Way, contains about two hundred fifty billion stars. Write this number in positional notation:

250000000000 stars

Answer:

• Two hundred fifty billion is:

b	illior	ıs	m	illioi	ns	the	ousai	$_{ m nds}$		units H	
Н	Т	U	Н	Т	U	Н	Т	U	Н	Т	U
2	5	0	0	0	0	0	0	0	0	0	0

• Two hundred fifty billion stars is 250 000 000 000 stars.

Ex 44: The approximate average distance between the Earth and the Sun is about one hundred fifty million kilometers. Write this number in positional notation:

150000000 kilometers

Answer:

• One hundred fifty million is:

b	illior	ıs	millions			the	ousai	$_{ m nds}$		units	U		
Η	Т	U	Н	H T U			Т	U	Н	Т	U		
0	0	0	1	5	0	0	0	0	0	0	0		

One hundred fifty million kilometers is 150 000 000 kilometers.

Ex 45: Throughout an average human lifetime, the heart beats approximately three billion times. Write this number in positional notation:



• Three billion is:

b	illior	ıs	m	illio	ıs	the	ousar	$_{ m nds}$	units		3
Н	Т	U	Н	Т	U	Н	Т	U	Н	Т	U
0	0	3	0	0	0	0	0	0	0	0	0

• Three billion heartbeats is 3000000000.

D COMPARING NUMBERS

D.1 COMPARING NUMBERS

Ex 46: Compare:

352 > 289

Answer:

- Both numbers have 3 digits. We proceed to compare the leftmost digit (hundreds place).
- The number 352 has a **3** in the hundreds place.
- The number 289 has a 2 in the hundreds place.
- Since 3 > 2, it is concluded that **352** > **289**. No further comparison is necessary.

Ex 47: Compare:

461 > 438

Answer:

- Both numbers have 3 digits. We compare from the leftmost digit
- The hundreds digits are identical (4). We proceed to the tens place.
- The number 461 has a **6** in the tens place.
- The number 438 has a **3** in the tens place.
- Since 6 > 3, it is concluded that 461 > 438.

Ex 48: Compare:

989 < 1023

Answer:

- First, we compare the number of digits.
- The number 989 has 3 digits.
- The number 1023 has 4 digits.
- The number with more digits is always greater.
- Therefore, it is concluded that 989 < 1023.

Ex 49: Compare:

8 4 5 6 < 8 4 5 9

Answer:

- Both numbers have 4 digits. We compare from the leftmost digit.
- The thousands digits are identical (8).
- The hundreds digits are identical (4).
- The tens digits are identical (5). We proceed to the ones place.
- The number 8456 has a **6** in the ones place.
- The number 8 459 has a **9** in the ones place.
- Since 6 < 9, it is concluded that 8456 < 8459.

Ex 50: Compare:

5109 > 5091

Answer:

- Both numbers have 4 digits. We compare from the leftmost digit.
- The thousands digits are identical (5). We proceed to the hundreds place.
- The number 5 109 has a 1 in the hundreds place.
- The number 5091 has a **0** in the hundreds place.
- Since 1 > 0, it is concluded that 5109 > 5091.

Ex 51: Compare:

23456 > 23198

Answer:

- Both numbers have 5 digits. We compare from the leftmost digit.
- The ten thousands digits are identical (2).
- The thousands digits are identical (3). We proceed to the hundreds place.
- The number 23 456 has a 4 in the hundreds place.
- The number 23 198 has a 1 in the hundreds place.
- Since 4 > 1, it is concluded that 23456 > 23198.

E BOUNDING A NUMBER

E.1 BOUNDING BY PLACE VALUE

Ex 52: Bound the number 482 by the nearest ten.

 $\boxed{480} \le 482 < \boxed{490}$

Answer:

• The target place value is the tens. The digit is 8.

- Lower Bound: Keep the digits to the left and the target digit (48), replace subsequent digits with zeros. The lower bound is 480.
- Upper Bound: Add 1 to the tens digit (8 + 1 = 9). The upper bound is 490.
- Therefore, 482 is bounded by 480 and 490.

So 480 < 482 < 490.

Ex 53: Bound the number 7291 by the nearest thousand.

$$7000 \le 7291 < 8000$$

Answer:

- The target place value is the thousands. The digit is 7.
- Lower Bound: Keep the 7, replace subsequent digits with zeros. The lower bound is 7000.
- **Upper Bound**: Add 1 to the thousands digit (7 + 1 = 8), replace subsequent digits with zeros. The upper bound is $8\,000$.
- Therefore, 7291 is bounded by 7000 and 8000.

So $7000 \le 7291 < 8000$.

Ex 54: Bound the number 5814 by the nearest hundred.

$$|5800| \le 5814 < 5900$$

Answer:

- The target place value is the hundreds. The digit is 8.
- Lower Bound: Keep the digits to the left and the target digit (58), replace subsequent digits with zeros. The lower bound is 5 800.
- Upper Bound: Add 1 to the hundreds digit (8 + 1 = 9). The upper bound is 5 900.
- Therefore, 5814 is bounded by 5800 and 5900.

So $5\,800 \le 5\,814 < 5\,900$.

Ex 55: Bound the number 45 678 by the nearest ten thousand.

$$\boxed{40000 \le 45\,678 < \boxed{50000}}$$

Answer:

- The target place value is the ten thousands. The digit is 4.
- Lower Bound: Keep the 4, replace subsequent digits with zeros. The lower bound is 40 000.
- Upper Bound: Add 1 to the ten thousands digit (4 + 1 = 5), replace subsequent digits with zeros. The upper bound is $50\,000$.
- Therefore, 45 678 is bounded by 40 000 and 50 000.

So $40\,000 \le 45\,678 < 50\,000$.

Ex 56: Bound the number 2956 by the nearest hundred.

$$\boxed{2900 \le 2956 < \boxed{3000}}$$

Answer:

- The target place value is the hundreds. The digit is 9.
- Lower Bound: Keep the digits to the left and the target digit (29), replace subsequent digits with zeros. The lower bound is 2 900.
- **Upper Bound**: Add 1 to the hundreds digit (9 + 1 = 10). This carries over, changing the thousands digit from 2 to 3. The upper bound is $3\,000$.
- Therefore, 2956 is bounded by 2900 and 3000.

So $2900 \le 2956 < 3000$.

Ex 57: Bound the number 8041 by the nearest hundred.

$$8000 \le 8041 < 8100$$

Answer:

- The target place value is the hundreds. The digit is 0.
- Lower Bound: Keep the digits to the left and the target digit (80), replace subsequent digits with zeros. The lower bound is 8 000.
- Upper Bound: Add 1 to the hundreds digit (0 + 1 = 1). The upper bound is 8 100.
- Therefore, 8041 is bounded by 8000 and 8100.

So $8000 \le 8041 < 8100$.

F ROUNDING NUMBERS

F.1 ROUNDING TO THE NEAREST TEN

Ex 58: Round the number 263 to the nearest ten.

$$263 \approx 260$$

Answer.

- 263 Find the digit in the tens place: 6
- 263 Look at the digit to the right: 3 Since 3 < 5, round down: 6 stays the same.
- 260 Replace all digits to the right with zeros.

$$263 \approx 260$$

Ex 59: Round the number 389 to the nearest ten.

$$389 \approx 390$$

Answer:

- 389 Find the digit in the tens place: 8
- 389 Look at the digit to the right: 9 Since $9 \ge 5$, round up: 8 + 1 = 9
- 390 Replace all digits to the right with zeros.

 $389 \approx 390$

Ex 60: Round the number 2342 to the nearest ten.

$$2342 \approx \boxed{2340}$$

2342 Find the digit in the tens place: 4

 $2\,3\underline{42}$ Look at the digit to the right: 2

Since 2 < 5, round down: 4 stays the same.

 $2\,340$ Replace all digits to the right with zeros.

 $2\,342\approx 2\,340$

Ex 61: Round the number 6779 to the nearest ten.

 $6779 \approx 6780$

Answer:

 $67\overline{2}9$ Find the digit in the tens place: 7

 $6\,77\underline{9}$ Look at the digit to the right: 9

Since $9 \ge 5$, round up: 7 + 1 = 8

6780 Replace all digits to the right with zeros.

 $6779 \approx 6780$

F.2 ROUNDING TO THE NEAREST HUNDRED

Ex 62: Round the number 365 to the nearest hundred.

 $365 \approx \boxed{400}$

Answer:

365 Find the digit in the hundreds place: 3

365 Look at the digit to the right: 6

Since $6 \ge 5$, round up by adding 1: 3 + 1 = 4

400 Replace all digits to the right with zeros.

 $365 \approx 400$

Ex 63: Round the number 2032 to the nearest hundred.

 $2032 \approx 2000$

Answer:

 $2\underline{0}32$ Find the digit in the hundreds place: 0

2032 Look at the digit to the right: 3

Since 3 < 5, round down: 0 stays the same.

2000 Replace all digits to the right with zeros.

 $2032 \approx 2000$

Ex 64: Round the number 35695 to the nearest hundred.

 $35\,695 \approx \boxed{35700}$

Answer:

35695 Find the digit in the hundreds place: 6

35695 Look at the digit to the right: 9

Since $9 \ge 5$, add 1: 6 + 1 = 7.

35700 Replace all digits to the right with zeros.

 $35\,695\approx35\,700$

Ex 65: Round the number 40 239 to the nearest hundred.

Answer:

 $40\underline{2}39$ Find the digit in the hundreds place: 2

 $402\underline{3}9$ Look at the digit to the right: 3

Since 3 < 5, round down: 2 stays the same.

40200 Replace all digits to the right with zeros.

 $40239 \approx 40200$

F.3 ROUNDING TO THE NEAREST THOUSAND

Ex 66: Round the number 23 100 to the nearest thousand.

 $23\,100 \approx \boxed{23000}$

Answer:

23 100 Find the digit in the thousands place: 3

 $23\underline{1}00$ Look at the digit to the right: 1

Since 1 < 5, round down: 3 stays the same.

23 000 Replace all digits to the right with zeros.

 $23\,100 \approx 23\,000$

Ex 67: Round the number 67645 to the nearest thousand.

 $67645 \approx \boxed{68000}$

Answer:

67 645 Find the digit in the thousands place: 7

67645 Look at the digit to the right: 6

Since $6 \ge 5$, round up: 7 + 1 = 8

68 000 Replace all digits to the right with zeros.

 $67645 \approx 68000$

Ex 68: Round the number 9 200 to the nearest thousand.

 $9\,200 \approx \boxed{9000}$

Answer:

9 200 Find the digit in the thousands place: 9

 $9\underline{2}00$ Look at the digit to the right: 2

Since 2 < 5, round down: 9 stays the same.

9000 Replace all digits to the right with zeros.

 $9\,200\approx 9\,000$

Ex 69: Round the number 9999 to the nearest thousand.

 $9999 \approx 10000$

Answer:

9999 Find the digit in the thousands place: 9

9999 Look at the digit to the right: 9

Since 9 > 5, round up: 9 + 1 = 10

10000 Replace all digits to the right with zeros.

 $9999 \approx 10000$