

# SOLVING QUADRATIC EQUATIONS

## A QUADRATIC EQUATION

### A.1 IDENTIFYING COEFFICIENTS OF QUADRATIC EQUATIONS: LEVEL 1

**Ex 1:** For the equation  $5x^2 - 2x - 3 = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

**Ex 2:** For the equation  $x^2 + 2x + 1 = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

**Ex 3:** For the equation  $-x^2 + 2 = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

**Ex 4:** For the equation  $-x^2 + 2x = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

### A.2 IDENTIFYING COEFFICIENTS OF QUADRATIC EQUATIONS: LEVEL 2

**Ex 5:** For the equation  $x^2 - x + 3 = 1$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

**Ex 6:** For the equation  $(x + 1)^2 = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

**Ex 7:** For the equation  $(x - 2)^2 + 2 = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

**Ex 8:** For the equation  $x(x - 2) = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

**Ex 9:** For the equation  $(x - 2)(x + 1) = 0$ , find the coefficients in the form  $ax^2 + bx + c = 0$ :

$$a = \square, b = \square \text{ and } c = \square$$

### A.3 RECOGNIZING QUADRATIC EQUATIONS

**MCQ 10:** Is the equation  $2x^2 - 3x + 2 = 0$  a quadratic equation?

☐ Yes.

☐ No.

**MCQ 11:** Is the equation  $2x - 3 = 0$  a quadratic equation?

☐ Yes.

☐ No.

**MCQ 12:** Is the equation  $2x^2 - 3x + \frac{1}{x} = 0$  a quadratic equation?

☐ Yes.

☐ No.

**MCQ 13:** Is the equation  $(x - 1)(x + 2) = 0$  a quadratic equation?

☐ Yes.

☐ No.

### A.4 VERIFYING ROOTS OF QUADRATIC EQUATIONS

**MCQ 14:** Is 1 a root of the equation  $x^2 - 2x + 1 = 0$ ?

☐ Yes.

☐ No.

**MCQ 15:** Is 1 a root of the equation  $x^2 + 2x + 1 = 0$ ?

☐ Yes.

☐ No.

**MCQ 16:** Is 2 a root of the equation  $(x - 1)(x - 2) = 0$ ?

☐ Yes.

☐ No.

**MCQ 17:** Is 5 a root of the equation  $(x - 2)^2 - 8 = 0$ ?

☐ Yes.

☐ No.

## B SOLVING BY FACTORIZATION

### B.1 FINDING SOLUTION SETS OF FACTORED QUADRATIC EQUATIONS

**MCQ 18:** For the equation  $(x - 1)(x + 2) = 0$ , the set of solutions is

☐  $S = \{-2, 1\}$

☐  $S = \{-1, 2\}$

☐  $S = \{2\}$

☐  $S = \{1\}$

**MCQ 19:** For the equation  $x(x - \sqrt{2}) = 0$ , the set of solutions is

☐  $S = \{0, -\sqrt{2}\}$

☐  $S = \{-\sqrt{2}\}$

☐  $S = \{0\}$

☐  $S = \{0, \sqrt{2}\}$

**MCQ 20:** For the equation  $(x - 1)^2 = 0$ , the set of solutions is

☐  $S = \{1\}$

☐  $S = \{-1\}$

☐  $S = \{1, -1\}$

☐  $S = \{0\}$

**MCQ 21:** For the equation  $(2x - 1)(x + 1) = 0$ , the set of solutions is

☐  $S = \{-1, 2\}$

☐  $S = \{\frac{1}{2}, -1\}$

☐  $S = \{2\}$

☐  $S = \{-1\}$

## B.2 SOLVING FACTORED QUADRATIC EQUATIONS

**Ex 22:** Solve the equation  $(x - 1)(x + 2) = 0$ . Justify your answer.

**Ex 23:** Solve the equation  $(x + 1)(x - 1) = 0$ . Justify your answer.

**Ex 24:** Solve the equation  $((x - 2) + 3)((x - 2) - 3) = 0$ . Justify your answer.

**Ex 25:** Solve the equation  $(x + \sqrt{2})(x - \sqrt{2}) = 0$ . Justify your answer.

## C FACTORIZATION TECHNIQUES FOR SPECIAL FORMS OF EQUATIONS

### C.1 FINDING SOLUTION SETS OF QUADRATIC EQUATIONS IN THE FORM $ax^2 + bx$

**MCQ 26:** For the equation  $x^2 + x = 0$ , the set of solutions is

☐  $S = \{-1, 0, 1\}$

☐  $S = \{1\}$

☐  $S = \{0\}$

☐  $S = \{0, -1\}$

**MCQ 27:** For the equation  $x^2 - 2x = 0$ , the set of solutions is

☐  $S = \{-2, 0\}$

☐  $S = \{2\}$

☐  $S = \{0\}$

☐  $S = \{0, 2\}$

**MCQ 28:** For the equation  $2x^2 + x = 0$ , the set of solutions is

☐  $S = \left\{-\frac{1}{2}, 0\right\}$

☐  $S = \{-2, 0\}$

☐  $S = \{2, 0\}$

☐  $S = \{0, 1\}$

**MCQ 29:** For the equation  $3x^2 = x$ , the set of solutions is

☐  $S = \{-3, 0\}$

☐  $S = \left\{0, \frac{1}{3}\right\}$

☐  $S = \{0, 3\}$

☐  $S = \{0, 1\}$

## C.2 SOLVING QUADRATIC EQUATIONS IN THE FORM $ax^2 + bx$

**Ex 30:** Solve the equation  $x^2 + x = 0$ . Justify your answer.

**Ex 31:** Solve the equation  $x^2 - 2x = 0$ . Justify your answer.

**Ex 32:** Solve the equation  $2x^2 - x = 0$ . Justify your answer.

**Ex 33:** Solve the equation  $2x^2 = 4x$ . Justify your answer.

## C.3 FINDING SOLUTION SETS OF QUADRATIC EQUATIONS IN THE FORM OF A DIFFERENCE OF SQUARES

**MCQ 34:** For the equation  $x^2 - 4 = 0$ , the set of solutions is

- ☐  $S = \{-4, 4\}$   
☐  $S = \{2\}$   
☐  $S = \{-1, 1\}$   
☐  $S = \{-2, 2\}$

**MCQ 35:** For the equation  $x^2 = -2$ , the set of solutions is

- ☐  $S = \{-2, 2\}$   
☐  $S = \{2\}$   
☐  $S = \{\}$   
☐  $S = \{-\sqrt{2}, \sqrt{2}\}$

**MCQ 36:** For the equation  $x^2 - 2 = 0$ , the set of solutions is

- ☐  $S = \{-\sqrt{2}, \sqrt{2}\}$   
☐  $S = \{-2, 2\}$   
☐  $S = \{2\}$   
☐  $S = \{-1, 1\}$

**MCQ 37:** For the equation  $(x-1)^2 - 9 = 0$ , the set of solutions is

- ☐  $S = \{-2, 4\}$   
☐  $S = \{-3, 3\}$   
☐  $S = \{2, 4\}$   
☐  $S = \{-1, 1\}$

**MCQ 38:** For the equation  $(x-1)^2 - 2 = 0$ , the set of solutions is

- ☐  $S = \{1 - \sqrt{2}, 1 + \sqrt{2}\}$   
☐  $S = \{-2, 4\}$   
☐  $S = \{-\sqrt{2}, \sqrt{2}\}$   
☐  $S = \{-1, 1\}$

## C.4 SOLVING QUADRATIC EQUATIONS IN THE FORM OF A DIFFERENCE OF SQUARES

**Ex 39:** Solve the equation  $x^2 - 4 = 0$ . Justify your answer.

**Ex 40:** Solve the equation  $x^2 = -2$ . Justify your answer.

**Ex 41:** Solve the equation  $x^2 - 2 = 0$ . Justify your answer.

☐  $S = \{-1, 3\}$

☐  $S = \{-1, 1\}$

**MCQ 45:** For the equation  $x^2 + 6x + 5 = 0$ , the set of solutions is

☐  $S = \{-5, -1\}$

☐  $S = \{-5, 1\}$

☐  $S = \{-1, 5\}$

☐  $S = \{1, 5\}$

**MCQ 46:** For the equation  $x^2 + 10x + 24 = 0$ , the set of solutions is

☐  $S = \{2, 4\}$

☐  $S = \{2, 6\}$

☐  $S = \{4, 6\}$

☐  $S = \{-4, -6\}$

**Ex 42:** Solve the equation  $(x-1)^2 - 9 = 0$ . Justify your answer.

**MCQ 47:** For the equation  $x^2 - 2x - 1 = 0$ , the set of solutions is

☐  $S = \{1 - \sqrt{2}, 1 + \sqrt{2}\}$

☐  $S = \{-1, 2\}$

☐  $S = \{-1, 1\}$

☐  $S = \{0, 2\}$

**Ex 43:** Solve the equation  $(x-1)^2 - 2 = 0$ . Justify your answer.

## D.2 SOLVING QUADRATIC EQUATIONS

**Ex 48:** Solve the equation  $x^2 + 2x - 3 = 0$ . Justify your answer.

**Ex 49:** Solve the equation  $x^2 + 6x + 5 = 0$ . Justify your answer.

## D THE GENERAL METHOD: COMPLETING THE SQUARE

### D.1 FINDING SOLUTION SETS OF QUADRATIC EQUATIONS

**MCQ 44:** For the equation  $x^2 + 2x - 3 = 0$ , the set of solutions is

☐  $S = \{-3, 1\}$

☐  $S = \{3, 1\}$

**Ex 50:** Solve the equation  $x^2 + 10x + 24 = 0$ . Justify your answer.

**Ex 51:** Solve the equation  $x^2 - 2x - 1 = 0$ . Justify your answer.

## E QUADRATIC FORMULA

### E.1 CALCULATING THE DISCRIMINANT

**Ex 52:** For the equation  $5x^2 - 2x - 3 = 0$ , calculate the discriminant:

$$\Delta = \square$$

**Ex 53:** For the equation  $x^2 + 6x + 5 = 0$ , calculate the discriminant:

$$\Delta = \square$$

**Ex 54:** For the equation  $2x^2 - x + 3 = 0$ , calculate the discriminant:

$$\Delta = \square$$

**Ex 55:** For the equation  $-2x^2 + 8 = 0$ , calculate the discriminant:

$$\Delta = \square$$

### E.2 SOLVING QUADRATIC EQUATIONS: STEP BY STEP

**Ex 56:** Consider the quadratic equation  $x^2 + 2x - 3 = 0$ .

1. Find the discriminant.

$$\Delta = \square$$

2. Hence, state the nature of the roots of the equation.  
☐ As  $\Delta > 0$ , there are 2 distinct roots.  
☐ As  $\Delta > 0$ , there is 1 single root.  
☐ As  $\Delta > 0$ , there are no roots.

3. The solutions of the equation are  and  (order from lowest to highest).

**Ex 57:** Consider the quadratic equation  $x^2 - 2x - 1 = 0$ .

1. Find the discriminant.

$$\Delta = \square$$

2. Hence, state the nature of the roots of the equation.  
☐ As  $\Delta > 0$ , there are 2 distinct roots.  
☐ As  $\Delta > 0$ , there is 1 single root.  
☐ As  $\Delta > 0$ , there are no roots.

3. The solutions of the equation are  and  (order from lowest to highest).

**Ex 58:** Consider the quadratic equation  $2x^2 - 3x + 1 = 0$ .

1. Find the discriminant.

$$\Delta = \square$$

2. Hence, state the nature of the roots of the equation.  
☐ As  $\Delta > 0$ , there are 2 distinct roots.  
☐ As  $\Delta > 0$ , there is 1 single root.  
☐ As  $\Delta > 0$ , there are no roots.

3. The solutions of the equation are  and  (order from lowest to highest).

**Ex 59:** Consider the quadratic equation  $2x^2 - 4x + 2 = 0$ .

1. Find the discriminant.

$$\Delta = \square$$

2. Hence, state the nature of the roots of the equation.  
☐ As  $\Delta = 0$ , there are 2 distinct roots.  
☐ As  $\Delta = 0$ , there are no real roots.  
☐ As  $\Delta = 0$ , there is 1 double root.

3. The solution of the equation is .

### E.3 SOLVING QUADRATIC EQUATIONS

**Ex 60:** Solve the quadratic equation  $x^2 + 2x - 3 = 0$ .

**Ex 61:** Solve the quadratic equation  $x^2 + 2x - 2 = 0$ .

**Ex 62:** Solve the quadratic equation  $x^2 - 2x + 6 = 0$ .

**Ex 65:** Solve the quadratic equation  $x^2 + 2x - 2 = 0$ .

**Ex 63:** Solve the quadratic equation  $x^2 - 6x + 9 = 0$ .

**Ex 66:** Solve the quadratic equation  $x^2 - 8x + 15 = 0$ .

#### E.4 SOLVING QUADRATIC EQUATIONS

**Ex 64:** Solve the quadratic equation  $2x^2 - 5x + 2 = 0$ .

**Ex 67:** Solve the quadratic equation  $x^2 + 6x + 5 = 0$ .

