

RATIOS

A WHAT IS A RATIO?

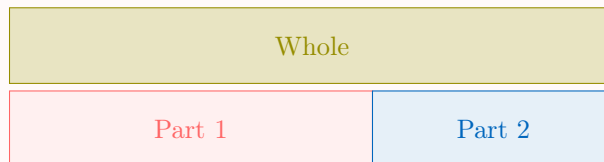
Definition Ratio

A **ratio** is a comparison of two quantities. The ratio of 2 to 3 can be expressed as the fraction $\frac{2}{3}$.

Definition Part-Part Ratio

A **part-part ratio** compares two distinct parts of a whole.

Part 1 : Part 2



Ex: A fruit bowl contains 3 cherries and 2 apples. What is the ratio of cherries to apples?



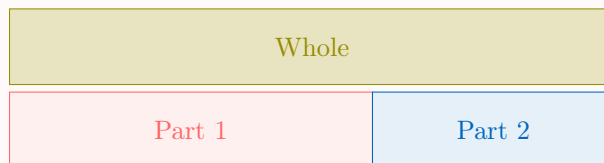
The ratio of cherries to apples is 3 : 2. This compares the two parts of the fruit collection to each other.

Answer: The ratio of cherries to apples is 3 : 2. This compares the two parts of the fruit collection to each other.

Definition Part-Whole Ratio

A **part-whole ratio** compares one part of a whole to the whole.

Part 1 : Whole or Part 2 : Whole



Ex: A juice is made with 1 lemon and 2 oranges. What is the ratio of oranges to the total number of fruits?



Answer:

- First, determine the total number of fruits. The total is $1 + 2 = 3$ fruits.
- The ratio of oranges (the part) to the total number of fruits (the whole) is 2 : 3.
- This part-to-whole ratio can also be expressed as the fraction $\frac{2}{3}$.

B EQUIVALENT RATIOS

Definition Equivalent Ratios

Two ratios are **equivalent** if they represent the same relationship. You can find equivalent ratios by multiplying or dividing both parts of the ratio by the same number.

Ex: The ratio of red apples to all apples is $\frac{2}{4}$, which is equivalent to $\frac{1}{2}$ (half of the apples are red).



Method Using Fractions

To check if two ratios are equivalent, we can compare their fractions. If the fractions are equivalent, then the ratios are equivalent.

Ex:

$$\text{Since } \frac{1}{2} = \frac{2}{4}, \text{ the ratios are equivalent: } 1 : 2 = 2 : 4$$

C PROPORTION

Definition Proportion

A **proportion** is an equation stating that two ratios are equivalent.

Ex: To make 1 chocolate cake, you need 4 eggs. How many eggs are needed for 2 cakes?

Answer: For 1 cake, you need 4 eggs. To find the number of eggs for 2 cakes, we set up a proportion:

$$\frac{4 \text{ eggs}}{1 \text{ cake}} = \frac{? \text{ eggs}}{2 \text{ cakes}}$$

By multiplying both parts of the ratio by 2, we find you need 8 eggs.

$$\frac{4 \text{ eggs}}{1 \text{ cake}} = \frac{8 \text{ eggs}}{2 \text{ cakes}}$$

D UNITARY METHOD

Method Unitary Method

If 5 apples cost \$10, how much do 8 apples cost?

- **Step 1: Find the cost of 1 apple (the unit cost).**
Divide the total cost by the number of apples.

$$\frac{\text{cost } \$10}{5 \text{ apples}} = \frac{\text{cost } \$2}{1 \text{ apple}}$$

One apple costs \$2.

- **Step 2: Find the cost of 8 apples.**
Multiply the unit cost by the number of apples you want.

$$\frac{\text{cost } \$2}{1 \text{ apple}} = \frac{\text{cost } \$16}{8 \text{ apples}}$$

So, 8 apples cost \$16.

E CROSS-MULTIPLICATION METHOD

Method Cross-Multiplication in Table

If 5 apples cost \$10, how much do 8 apples cost?

- **Step 1: Set up the table.** Organize the information with matching units in the same row.

Price (\$)	10	?
Number of Apples	5	8

- **Step 2: Cross-multiply and divide.** Multiply the two numbers that are diagonal to each other, and then divide by the remaining number.

Price (\$)	10 ÷	$\frac{8 \times 10}{5} = 16$
Number of Apples	5 ×	8

- So, 8 apples cost \$16.

Method Cross-Multiplication with Fractions

If 5 apples cost \$10, how much do 8 apples cost?

- **Step 1: Set up the proportion.** Let x be the unknown cost.

$$\frac{\$10}{5 \text{ apples}} = \frac{\$x}{8 \text{ apples}}$$

- **Step 2: Cross-multiply and solve for x .** Multiply the numbers that are diagonal to each other.

$$\begin{array}{l} \frac{10}{5} = \frac{x}{8} \\ 5 \times x = 10 \times 8 \quad (\text{cross multiplication}) \\ x = 10 \times 8 \div 5 \quad (\text{dividing both sides by } 5) \\ x = 16 \end{array}$$

- So, 8 apples cost \$16.