

INTEGERS

A DEFINITION

A.1 COUNTING POSITIVE AND NEGATIVE NUMBERS

Ex 1:

$$\textcircled{+} \textcircled{+} = \boxed{+2}$$

Answer:

- There are 2 positive units.

$$\bullet \textcircled{+} \textcircled{+} = +2$$

Ex 2:

$$\textcircled{-} \textcircled{-} \textcircled{-} = \boxed{-3}$$

Answer:

- There are 3 negative units.

$$\bullet \textcircled{-} \textcircled{-} \textcircled{-} = -3$$

Ex 3:

$$\textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} = \boxed{-5}$$

Answer:

- There are 5 negative units.

$$\bullet \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} = -5$$

Ex 4:

$$\textcircled{+} \textcircled{+} \textcircled{+} = \boxed{+3}$$

Answer:

- There are 3 positive units.

$$\bullet \textcircled{+} \textcircled{+} \textcircled{+} = +3$$

Ex 5:

$$\textcircled{-} = \boxed{-1}$$

Answer:

- There is 1 negative unit.

$$\bullet \textcircled{-} = -1$$

A.2 WRITING INTEGERS FROM WORDS

Ex 6: Positive two is $\boxed{+2}$.

Answer:

- Positive two is $+2 = \textcircled{+} \textcircled{+}$

Ex 7: Negative three is $\boxed{-3}$.

Answer:

- Negative three is $-3 = \textcircled{-} \textcircled{-} \textcircled{-}$

Ex 8: Negative four is $\boxed{-4}$.

Answer:

- Negative four is $-4 = \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-}$

Ex 9: Positive five is $\boxed{+5}$.

Answer:

- Positive five is $+5 = \textcircled{+} \textcircled{+} \textcircled{+} \textcircled{+} \textcircled{+}$

Ex 10: Negative two is $\boxed{-2}$.

Answer:

- Negative two is $-2 = \textcircled{-} \textcircled{-}$

A.3 FINDING THE OPPOSITE

Ex 11: The opposite of -4 is $\boxed{+4}$.

Answer:

$$\bullet \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} + \textcircled{+} \textcircled{+} \textcircled{+} \textcircled{+} = \textcircled{-} \textcircled{+} \textcircled{-} \textcircled{+} \textcircled{-} \textcircled{+}$$

$$\bullet (-4) + (+4) = 0$$

- The opposite of -4 is $+4$.

Ex 12: The opposite of -3 is $\boxed{+3}$.

Answer:

$$\bullet \textcircled{-} \textcircled{-} \textcircled{-} + \textcircled{+} \textcircled{+} \textcircled{+} = \textcircled{-} \textcircled{+} \textcircled{-} \textcircled{+}$$

$$\bullet (-3) + (+3) = 0$$

- The opposite of -3 is $+3$.

Ex 13: The opposite of $+5$ is $\boxed{-5}$.

Answer:

$$\bullet \textcircled{+} \textcircled{+} \textcircled{+} \textcircled{+} \textcircled{+} + \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} = \textcircled{-} \textcircled{+} \textcircled{-} \textcircled{+} \textcircled{-} \textcircled{+}$$

$$\bullet (+5) + (-5) = 0$$

- The opposite of $+5$ is -5 .

Ex 14: The opposite of $+1$ is $\boxed{-1}$.

Answer:

- $\oplus + \ominus = \omin�$

- $(+1) + (-1) = 0$

- The opposite of $+1$ is -1 .

Ex 15: The opposite of 0 is $\boxed{0}$.

Answer:

- $\overset{0}{\oplus} + \overset{0}{\ominus} = \overset{0}{\omin�}$

- $0 + 0 = 0$

- The opposite of 0 is 0.

A.4 FINDING THE OPPOSITE FOR DECIMAL NUMBERS

Ex 16: The opposite of -4.1 is $\boxed{+4.1}$.

Answer:

- $(-4.1) + (+4.1) = 0$

- The opposite of $-4,1$ is $+4,1$.

Ex 17: The opposite of -0.5 is $\boxed{+0.5}$.

Answer:

- $(-0.5) + (+0.5) = 0$

- The opposite of $-0,5$ is $+0,5$.

Ex 18: The opposite of $+3.5$ is $\boxed{-3.5}$.

Answer:

- $(+3.5) + (-3.5) = 0$

- The opposite of $+3,5$ is $-3,5$.

Ex 19: The opposite of $+99.5$ is $\boxed{-99.5}$.

Answer:

- $99.5 = +99.5$

- $(+99.5) + (-99.5) = 0$

- The opposite of $+99,5$ is $-99,5$.

A.5 ADDING SMALL INTEGERS

Ex 20: $(+1) + (-2) = \boxed{-1}$

Answer:

- $\oplus + \ominus \ominus = \omin� \omin�$
= $\omin�$

- $(+1) + (-2) = -1$

Ex 21: $(+3) + (-1) = \boxed{+2}$

Answer:

- $\oplus \oplus \oplus + \ominus = \oplus \oplus \omin�$
= $\oplus \oplus$

- $(+3) + (-1) = +2$

Ex 22: $(+2) + (-3) = \boxed{-1}$

Answer:

- $\oplus \oplus + \omin� \omin� \omin� = \omin� \omin� \omin�$
= $\omin�$

- $(+2) + (-3) = -1$

Ex 23: $(-2) + (-1) = \boxed{-3}$

Answer:

- $\omin� \omin� + \omin� = \omin� \omin� \omin�$

- $(-2) + (-1) = -3$

Ex 24: $(-1) + (+3) = \boxed{+2}$

Answer:

- $\omin� + \oplus \oplus \oplus = \oplus \oplus \omin�$
= $\oplus \oplus$

- $(-1) + (+3) = +2$

Ex 25: $(+2) + (+3) = \boxed{+5}$

Answer:

- $\oplus \oplus + \oplus \oplus \oplus = \oplus \oplus \oplus \oplus \oplus$

- $(+2) + (+3) = +5$

A.6 FINDING MISSING NUMBERS IN ADDITION

Ex 26: $(+3) + (\boxed{-2}) = +1$

Answer:

- $\oplus \oplus \oplus + \omin� \omin� = \oplus \omin� \omin�$
= \oplus

- $(+3) + (-2) = +1$

Ex 27: $(-4) + (\boxed{+2}) = -2$

Answer:

- $\omin� \omin� \omin� \omin� + \oplus \oplus = \omin� \omin� \omin� \omin� \oplus \oplus$
= $\omin� \omin�$

- $(-4) + (+2) = -2$

Ex 28: $(\boxed{-3}) + (+2) = -1$

Answer:

B RULES OF ADDITION

B.1 ADDING INTEGERS

Ex 41: $(+6) + (-4) = \boxed{+2}$

Answer:

- When the signs are opposite, subtract the absolute values ($6 - 4 = 2$), and take the sign of the larger number: $6 > 4$, so the result is $+$.

- $(+6) + (-4) = +2$



Ex 42: $(+4) + (+7) = \boxed{+11}$

Answer:

- When the signs are the same, add the absolute values ($4 + 7 = 11$), and keep the positive sign.

- $(+4) + (+7) = +11$



Ex 43: $(-5) + (+8) = \boxed{+3}$

Answer:

- When the signs are opposite, subtract the absolute values ($8 - 5 = 3$), and take the sign of the larger number: $8 > 5$, so the result is $+$.

- $(-5) + (+8) = +3$



Ex 44: $(+6) + (-4) = \boxed{+2}$

Answer:

- When the signs are opposite, subtract the absolute values ($6 - 4 = 2$), and take the sign of the larger number: $6 > 4$, so the result is $+$.

- $(+6) + (-4) = +2$

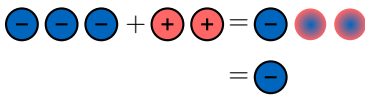


Ex 45: $(-5) + (-4) = \boxed{-9}$

Answer:

- When the signs are the same, add the absolute values ($5 + 4 = 9$), and keep the negative sign.

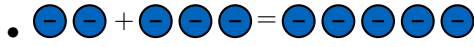
- $(-5) + (-4) = -9$



- $(-3) + (+2) = -1$

Ex 29: $(-2) + (-3) = -5$

Answer:



- $(-2) + (-3) = -5$

Ex 30: $(+2) + (+1) = +3$

Answer:



- $(+2) + (+1) = +3$

Ex 31: $(+2) + (-5) = -3$

Answer:



- $(+2) + (-5) = -3$

A.7 FINDING THE ABSOLUTE VALUE

Ex 32: The absolute value of $+2$ is $\boxed{2}$.

Answer: The absolute value of $+2 = \textcircled{+} \textcircled{+}$ is 2.

Ex 33: The absolute value of -3 is $\boxed{3}$.

Answer: The absolute value of $-3 = \textcircled{-} \textcircled{-} \textcircled{-}$ is 3.

Ex 34: The absolute value of $+5$ is $\boxed{5}$.

Answer: The absolute value of $+5 = \textcircled{+} \textcircled{+} \textcircled{+} \textcircled{+} \textcircled{+}$ is 5.

Ex 35: The absolute value of -4 is $\boxed{4}$.

Answer: The absolute value of $-4 = \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-}$ is 4.

Ex 36: The absolute value of -9 is $\boxed{9}$.

Answer: The absolute value of $-9 = \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-}$ is 9.

A.8 FINDING THE ABSOLUTE VALUE FOR DECIMAL NUMBERS

Ex 37: The absolute value of -2.1 is $\boxed{2.1}$.

Answer: The absolute value of -2.1 is 2.1

Ex 38: The absolute value of -5.4 is $\boxed{5.4}$.

Answer: The absolute value of -5.4 is 5.4.

Ex 39: The absolute value of 3.7 is $\boxed{3.7}$.

Answer: The absolute value of 3.7 is 3.7.

Ex 40: The absolute value of 0 is $\boxed{0}$.

Answer: The absolute value of 0 is 0.

B.2 ADDING INTEGERS WITHOUT EXPLICIT SIGNS

Ex 46: $6 + (-4) = \boxed{+2}$

Answer:

- $6 + (-4) = (+6) + (-4)$
- When the signs are opposite, subtract the absolute values ($6 - 4 = 2$), and take the sign of the larger number: $6 > 4$, so the result is $+$.
- $(+6) + (-4) = +2$



Ex 47: $-5 + 8 = \boxed{+3}$

Answer:

- $-5 + 8 = (-5) + (+8)$
- When the signs are opposite, subtract the absolute values ($8 - 5 = 3$), and take the sign of the larger number: $8 > 5$, so the result is $+$.
- $(-5) + (+8) = +3$



Ex 48: $-2 + (-3) = \boxed{-5}$

Answer:

- $-2 + (-3) = (-2) + (-3)$
- When the signs are the same, add the absolute values ($2 + 3 = 5$), and keep the negative sign.
- $(-2) + (-3) = -5$
-

Ex 49: $-6 + 0 = \boxed{-6}$

Answer:

- $-6 + 0 = (-6) + 0$
- Adding zero to any number does not change the value, so the result is -6 .
- $(-6) + 0 = -6$

B.3 ADDING SIGNED DECIMAL NUMBERS

Ex 50: $-5 + 8.1 = \boxed{+3.1}$

Answer:

- $-5 + 8.1 = (-5) + (+8.1)$
- When the signs are opposite, subtract the absolute values ($8.1 - 5 = 3.1$), and take the sign of the larger number: $8.1 > 5$, so the result is $+$.
- $(-5) + (+8.1) = +3.1$

Ex 51: $-3 + (-2.5) = \boxed{-5.5}$

Answer:

- $-3 + (-2.5) = (-3) + (-2.5)$
- When the signs are the same, add the absolute values ($3 + 2.5 = 5.5$), and keep the negative sign.
- $(-3) + (-2.5) = -5.5$

Ex 52: $-1.6 + (+2.6) = \boxed{+1}$

Answer:

- $-1.6 + (+2.6) = (-1.6) + (+2.6)$
- When the signs are opposite, subtract the absolute values ($2.6 - 1.6 = 1.0$), and take the sign of the larger number: $2.6 > 1.6$, so the result is $+$.
- $(-1.6) + (+2.6) = +1.0$

Ex 53: $-3.5 + (+1.5) = \boxed{-2}$

Answer:

- $-3.5 + (+1.5) = (-3.5) + (+1.5)$
- When the signs are opposite, subtract the absolute values ($3.5 - 1.5 = 2.0$), and take the sign of the larger number: $3.5 > 1.5$, so the result is $-$.
- $(-3.5) + (+1.5) = -2.0$

B.4 ADDING MULTIPLE INTEGERS

Ex 54: Calculate:

$$(+3) + (-7) + (-5) = \boxed{-9}$$

Answer:

$$\begin{aligned} (+3) + (-7) + (-5) &= (-4) + (-5) && ((+3)+(-7)=(-4)) \\ &= (-9) && ((-4)+(-5)=(-9)) \end{aligned}$$

Ex 55: Calculate:

$$(-2) + (-4) + (+7) = \boxed{+1}$$

Answer:

$$\begin{aligned} (-2) + (-4) + (+7) &= (-6) + (+7) && ((-2)+(-4)=(-6)) \\ &= +1 && ((-6)+(+7)=+1) \end{aligned}$$

Ex 56: Calculate:

$$(-2) + (+4) + (-2) = \boxed{0}$$

Answer:

$$\begin{aligned} (-2) + (+4) + (-2) &= (+2) + (-2) && ((-2)+(+4)=+2) \\ &= 0 && ((+2)+(-2)=0) \end{aligned}$$

Ex 57: Calculate:

$$(-10) + (+3) + (-7) = \boxed{-14}$$

Answer:

$$\begin{aligned} (-10) + (+3) + (-7) &= (-7) + (-7) && ((-10)+(+3)=-7) \\ &= -14 && ((-7)+(-7)=-14) \end{aligned}$$

B.5 ADDING INTEGERS IN REAL-WORLD PROBLEMS

Ex 58: During a hike, the hiker experiences altitude changes as follows. Positive numbers indicate climbing (gaining altitude), while negative numbers indicate descending (losing altitude):

- The hiker starts at an altitude of +300 meters.
- They climb +150 meters in the morning.
- In the afternoon, they descend by -200 meters.

What is the hiker's final altitude at the end of the day?

$$\boxed{250} \text{ meters}$$

Answer:

$$\begin{aligned} (+300) + (+150) + (-200) &= (+450) + (-200) && ((+300)+(+150)=+450) \\ &= +250 && ((+450)+(-200)=+250) \end{aligned}$$

Ex 59: A person keeps track of their bank account balance as follows. Positive numbers indicate deposits (money added), while negative numbers indicate withdrawals (money taken out):

- The person starts with +50 dollars in their account.
- They deposit +30 dollars.
- Later, they withdraw -40 dollars.

What is the person's final balance?

$$\boxed{40} \text{ dollars}$$

Answer:

$$\begin{aligned} (+50) + (+30) + (-40) &= (+80) + (-40) && ((+50)+(+30)=+80) \\ &= +40 && ((+80)+(-40)=+40) \end{aligned}$$

Ex 60: In a round of golf, each hole has a "par" score, and a player's score is based on how many strokes they take compared to par. A score of 0 means the player made par, a positive number means they took extra strokes (over par), and a negative number means they made fewer strokes (under par).

- Hole 1: Par 3, player scored -1 (under par)
- Hole 2: Par 4, player scored +2 (over par)
- Hole 3: Par 5, player scored 0 (made par)
- Hole 4: Par 3, player scored +1 (over par)
- Hole 5: Par 4, player scored -2 (under par)

What is the player's total score?

$$\boxed{0}$$

Answer:

$$\begin{aligned} (-1) + (+2) + (0) + (+1) + (-2) &= (+1) + (0) + (+1) + (-2) && ((-1)+(+2)=(+1)) \\ &= (+1) + (+1) + (-2) && ((+1)+(0)=(+1)) \\ &= (+2) + (-2) && ((+1)+(+1)=(+2)) \\ &= 0 && ((+2)+(-2)=0) \end{aligned}$$

Ex 61: Throughout the day, the temperature in a city changes as follows. Positive numbers indicate a rise in temperature, while negative numbers indicate a drop in temperature:

- In the morning, the temperature started at +5°C and dropped by -3°C.
- In the afternoon, the temperature rose by +4°C.
- In the evening, the temperature dropped again by -6°C.
- At night, it dropped further by -1°C.

What is the temperature at the end of the day?

$$\boxed{-1}^{\circ}\text{C}$$

Answer:

$$\begin{aligned} (+5) + (-3) + (+4) + (-6) + (-1) &= (+2) + (+4) + (-6) + (-1) && ((+5)+(-3)=(+2)) \\ &= (+6) + (-6) + (-1) && ((+2)+(+4)=(+6)) \\ &= 0 + (-1) && ((+6)+(-6)=0) \\ &= -1 && (0+(-1)=-1) \end{aligned}$$

C SUBTRACTION

C.1 CONVERTING SUBTRACTION TO ADDITION

Ex 62: Convert the subtracting in addition:

$$(+4) - (+2) = \boxed{+4} + \boxed{-2}$$

Answer:

- $(+4) - (+2) = (+4) + (-2)$
-

Ex 63: Convert the subtraction into addition:

$$(-5) - (-3) = \boxed{-5} + \boxed{+3}$$

Answer:

- $(-5) - (-3) = (-5) + (+3)$
-

Ex 64: Convert the subtraction into addition:

$$(+4) - (-2) = \boxed{+4} + \boxed{+2}$$

Answer:

- $(+4) - (-2) = (+4) + (+2)$
-

Ex 65: Convert the subtraction into addition:

$$(-1) - (+2) = \boxed{-1} + \boxed{-2}$$

Answer:

- $(-1) - (+2) = (-1) + (-2)$
-

C.2 SUBTRACTING INTEGERS STEP BY STEP

Ex 66: Calculate:

$$\begin{aligned} (+4) - (+2) &= (\boxed{+4}) + (\boxed{-2}) \\ &= \boxed{2} \end{aligned}$$

Answer:

- $(+4) - (+2) = (+4) + (-2)$
 $= (+2)$

Ex 67: Calculate:

$$\begin{aligned} (-2) - (-3) &= (\boxed{-2}) + (\boxed{+3}) \\ &= \boxed{+1} \end{aligned}$$

Answer:

- $(-2) - (-3) = (-2) + (+3)$
 $= (+1)$

Ex 68: Calculate:

$$\begin{aligned} (-4) - (+2) &= (\boxed{-4}) + (\boxed{-2}) \\ &= \boxed{-6} \end{aligned}$$

Answer:

- $(-4) - (+2) = (-4) + (-2)$
 $= (-6)$

Ex 69: Calculate:

$$\begin{aligned} (+3) - (-2) &= (\boxed{+3}) + (\boxed{+2}) \\ &= \boxed{+5} \end{aligned}$$

Answer:

- $(+3) - (-2) = (+3) + (+2)$
 $= (+5)$

C.3 SUBTRACTING INTEGERS

Ex 70: Calculate:

$$(+4) - (+2) = \boxed{2}$$

Answer:

- $(+4) - (+2) = (+4) + (-2)$
 $= (+2)$

Ex 71: Calculate:

$$(-2) - (-4) = \boxed{+2}$$

Answer:

- $(-2) - (-4) = (-2) + (+4)$
 $= (+2)$

Ex 72: Calculate:

$$(+2) - (-3) = \boxed{+5}$$

Answer:

- $(+2) - (-3) = (+2) + (+3)$
 $= (+5)$

Ex 73: Calculate:

$$(-3) - (+4) = \boxed{-7}$$

Answer:

- $(-3) - (+4) = (-3) + (-4)$
 $= (-7)$

C.4 SUBTRACTING INTEGERS WITHOUT EXPLICIT SIGNS

Ex 74: Calculate:

$$3 - (-2) = \boxed{5}$$

Answer:

- $3 - (-2) = (+3) - (-2)$
 $= (+3) + (+2)$
 $= (+5)$

$$\begin{aligned} (+) (+) (+) (-) (-) &= (+) (+) (+) (+) (+) \\ &= (+) (+) (+) (+) (+) \end{aligned}$$

Ex 75: Calculate:

$$(-2) - 3 = \boxed{-5}$$

Answer:

$$\begin{aligned} (-2) - 3 &= (-2) - (+3) \\ &= (-2) + (-3) \\ &= (-5) \end{aligned}$$

$$\begin{aligned} (-) (-) (-) (+) (+) &= (-) (-) (-) (-) (-) \\ &= (-) (-) (-) (-) (-) \end{aligned}$$

Ex 76: Calculate:

$$(-3) - (-5) = \boxed{+2}$$

Answer:

$$\begin{aligned} (-3) - (-5) &= (-3) - (-5) \\ &= (-3) + (+5) \\ &= (+2) \end{aligned}$$

$$\begin{aligned} (-) (-) (-) (-) (-) (-) (-) &= (-) (-) (-) (+) (+) (+) (+) (+) \\ &= (+) (+) \end{aligned}$$

Ex 77: Calculate:

$$3 - 5 = \boxed{-2}$$

Answer:

$$\begin{aligned} 3 - 5 &= (+3) - (+5) \\ &= (+3) + (-5) \\ &= (-2) \end{aligned}$$

$$\begin{aligned} (+) (+) (+) (-) (-) (-) (-) (-) &= (+) (+) (+) (-) (-) (-) (-) \\ &= (-) (-) \end{aligned}$$

C.5 ADDING/SUBTRACTING MULTIPLE INTEGERS

Ex 78: Calculate:

$$(+3) - (-7) - (+5) = \boxed{+5}$$

Answer:

$$\begin{aligned} (+3) - (-7) - (+5) &= (+3) + (+7) + (-5) && \text{(subtraction to addition)} \\ &= (+10) + (-5) && ((+3)+(+7)=(+10)) \\ &= (+5) && ((+10)+(-5)=(+5)) \end{aligned}$$

Ex 79: Calculate:

$$(-2) - (-3) + (-2) = \boxed{-1}$$

Answer:

$$\begin{aligned} (-2) - (-3) + (-2) &= (-2) + (+3) + (-2) && \text{(subtraction to addition)} \\ &= (+1) + (-2) && ((-2)+(+3)=(+1)) \\ &= (-1) && ((+1)+(-2)=(-1)) \end{aligned}$$

Ex 80: Calculate:

$$(-5) - (-4) + (-3) = \boxed{-4}$$

Answer:

$$\begin{aligned} (-5) - (-4) + (-3) &= (-5) + (+4) + (-3) && \text{(subtraction to addition)} \\ &= (-1) + (-3) && ((-5)+(+4)=(-1)) \\ &= (-4) && ((-1)+(-3)=(-4)) \end{aligned}$$

Ex 81: Calculate:

$$(+6) - (-3) + (-4) = \boxed{+5}$$

Answer:

$$\begin{aligned} (+6) - (-3) + (-4) &= (+6) + (+3) + (-4) && \text{(subtraction to addition)} \\ &= (+9) + (-4) && ((+6)+(+3)=(+9)) \\ &= (+5) && ((+9)+(-4)=(+5)) \end{aligned}$$

C.6 SUBTRACTING INTEGERS IN REAL-WORLD PROBLEMS

Ex 82: In the morning, the temperature was -7°C , and by the evening, the temperature was -2°C . Find the variation of temperature.

$$\boxed{5}^{\circ}\text{C}$$

Answer:

$$\begin{aligned} \text{Temperature variation} &= \text{Final Temperature} - \text{Initial Temperature} \\ &= (-2) - (-7) \\ &= (-2) + (+7) && \text{(subtraction to addition)} \\ &= +5^{\circ}\text{C} \end{aligned}$$

Ex 83: In the morning, your bank account balance was -50 dollars, and by the evening, it was $+30$ dollars. Find the change in your bank account balance.

$$\boxed{80} \text{ dollars}$$

Answer:

$$\begin{aligned} \text{Change in Balance} &= \text{Final Balance} - \text{Initial Balance} \\ &= 30 - (-50) \\ &= 30 + 50 && \text{(subtraction to addition)} \\ &= 80 \text{ dollars} \end{aligned}$$

Ex 84: A lift starts at the 5th floor and descends to the -2nd floor (below ground level). Find the change in the lift's position.

$$\boxed{-7} \text{ floors}$$

Answer:

$$\begin{aligned} \text{Change in Position} &= \text{Final Floor} - \text{Initial Floor} \\ &= (-2) - 5 \\ &= (-2) + (-5) && \text{(subtraction to addition)} \\ &= -7 \text{ floors} \end{aligned}$$

Ex 85: The GDP (Gross Domestic Product) growth rate of a country was -2% in 2024. It was $+3\%$ in 2025. Find the variation in the GDP growth rate.

$\boxed{5}\%$

Answer:

$$\text{GDP Variation} = \text{Final GDP} - \text{Initial GDP}$$

$$\text{Variation du PIB} = \text{Taux de croissance final du PIB} - \text{Taux de croissance initial du PIB}$$

$$= (+3) - (-2)$$

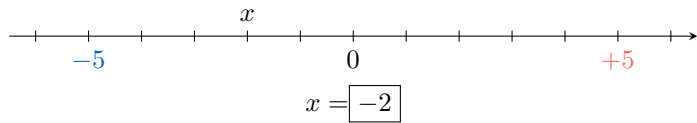
$$= (+3) + (+2) \quad (\text{subtraction to addition})$$

$$= +5\%$$

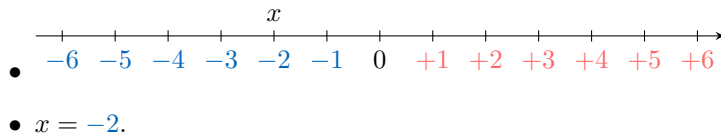
D ON THE NUMBER LINE

D.1 FINDING X ON THE NUMBER LINE

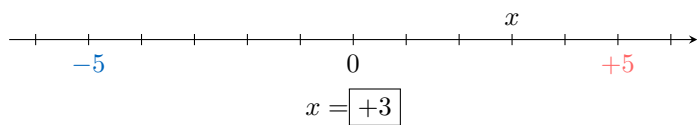
Ex 86: Find the value of x .



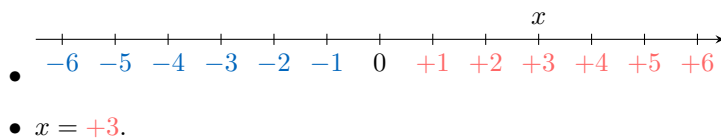
Answer:



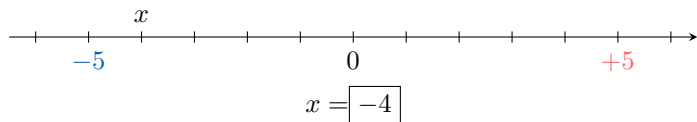
Ex 87: Find the value of x .



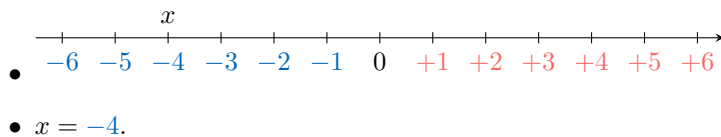
Answer:



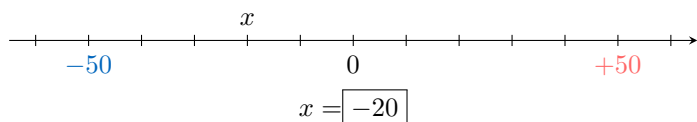
Ex 88: Find the value of x .



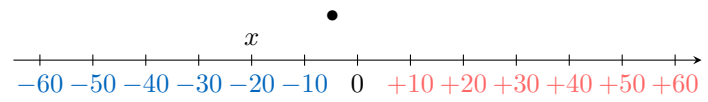
Answer:



Ex 89: Find the value of x .

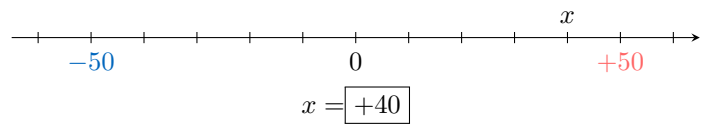


Answer:

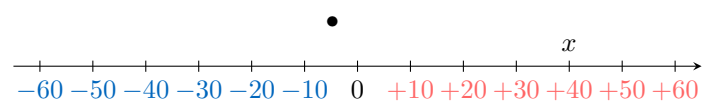


$\bullet x = -20.$

Ex 90: Find the value of x .

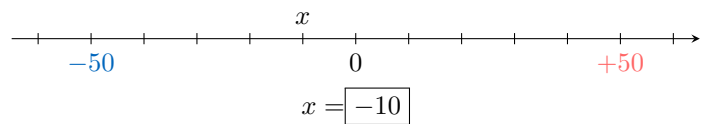


Answer:

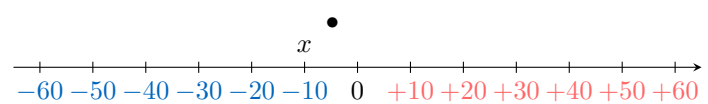


$\bullet x = +40.$

Ex 91: Find the value of x .



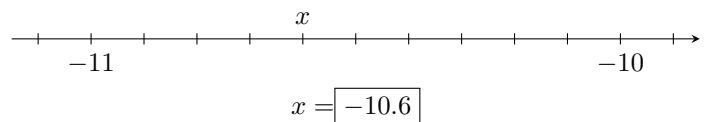
Answer:



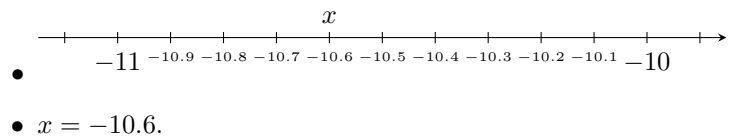
$\bullet x = -10.$

D.2 FINDING DECIMAL NUMBERS ON THE NUMBER LINE

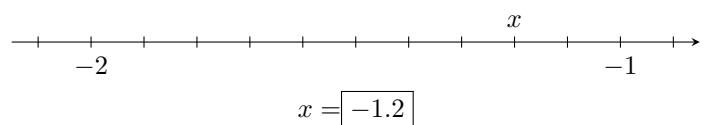
Ex 92: Find the value of x .



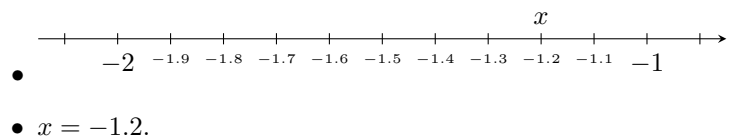
Answer:



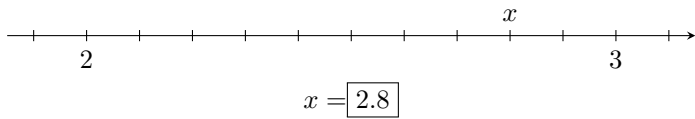
Ex 93: Find the value of x .



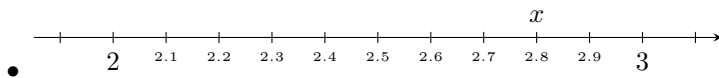
Answer:



Ex 94: Find the value of x .

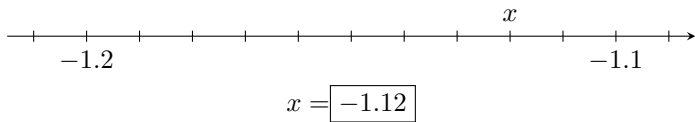


Answer:

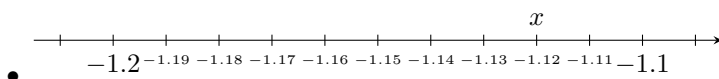


- $x = 2.8$.

Ex 95: Find the value of x .



Answer:



- $x = -1.12$.

E ORDERING

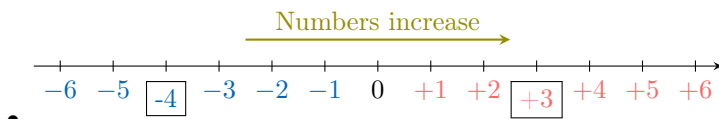
E.1 COMPARING SMALL INTEGERS

Ex 96: Compare the numbers: $-4 < +3$

Answer:

- $+3$ is positive, and -4 is negative. A positive number is always greater than a negative number:

$$-4 < +3$$

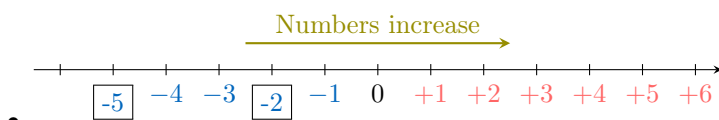


Ex 97: Compare the numbers: $-2 > -5$

Answer:

- Both numbers are negative, but -2 is closer to zero than -5 . Therefore, -2 is greater than -5 :

$$-2 > -5$$

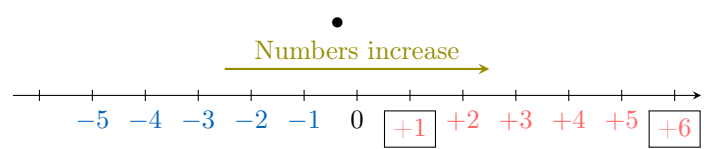


Ex 98: Compare the numbers: $+6 > +1$

Answer:

- Both numbers are positive, but $+6$ is farther from zero than $+1$. Therefore, $+6$ is greater than $+1$:

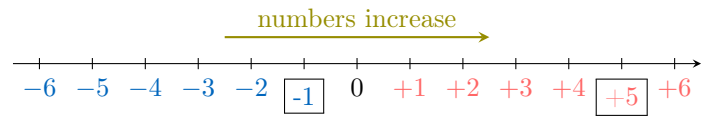
$$+6 > +1$$



Ex 99: Compare: $-1 < +5$

Answer:

- As $+5$ is positive and -1 is negative, the positive number is greater than the negative number: $-1 < +5$

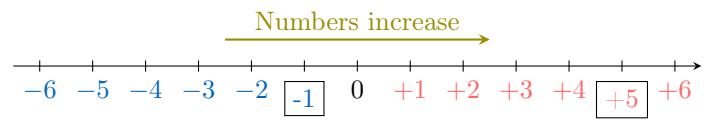


Ex 100: Compare the numbers: $-1 < +5$

Answer:

- $+5$ is positive and -1 is negative. A positive number is always greater than a negative number:

$$-1 < +5$$

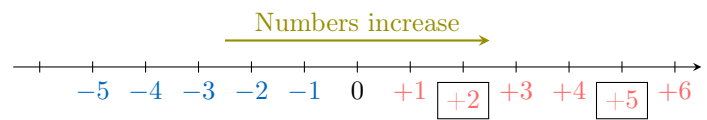


Ex 101: Compare the numbers: $+2 < +5$

Answer:

- Both numbers are positive, but $+5$ is farther from zero than $+2$:

$$+2 < +5$$

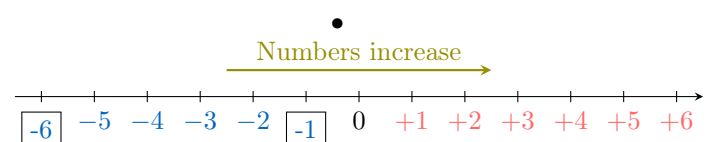


Ex 102: Compare the numbers: $-6 < -1$

Answer:

- Both numbers are negative, but -1 is closer to zero than -6 :

$$-6 < -1$$



E.2 COMPARING INTEGERS

Ex 103: Compare the numbers: $-20 \boxed{<} 1$

Answer:

- 1 is positive and -20 is negative. A positive number is always greater than a negative number:

$$-20 < +1$$

Ex 104: Compare the numbers: $-99 \boxed{>} -100$

Answer:

- Both numbers are negative, but -99 is closer to zero than -100 :

$$-99 > -100$$

Ex 105: Compare the numbers: $234 \boxed{>} -1200$

Answer:

- $+234$ is positive and -1200 is negative. A positive number is always greater than a negative number:

$$+234 > -1200$$

Ex 106: Compare the numbers: $-18 \boxed{<} -3$

Answer:

- Both numbers are negative, but -3 is closer to zero than -18 :

$$-18 < -3$$

Ex 107: Compare the numbers: $230 \boxed{>} 200$

Answer:

- Both numbers are positive, but $+230$ is farther from zero than $+200$:

$$+230 > +200$$

Ex 108: Compare the numbers: $99 \boxed{>} -100$

Answer:

- $+99$ is positive and -100 is negative. A positive number is always greater than a negative number:

$$+99 > -100$$

E.3 COMPARING INTEGERS IN REAL-WORLD PROBLEMS

MCQ 109: During a golf tournament, the scores relative to par for five different holes were:

$$-2, -1, 0, +1, -3$$

Order these scores from the best performance (most under par) to the worst performance (above par).

Choose one answer:

$0 < +1 < -1 < -2 < -3$

$-3 < -2 < -1 < 0 < +1$

$+1 > 0 > -1 > -2 > -3$

$-1 < -2 < -3 < 0 < +1$

Answer:

- From the best performance to the worst: $-3 < -2 < -1 < 0 < +1$

MCQ 110: Given the depths of various lakes below sea level:

Lake	Depth below sea level
Lake Assal, Djibouti	-155 m
Death Valley, USA	-86 m
Caspian Sea, Central Asia	-28 m
Sea of Galilee, Israel	-214 m

Which lake is the deepest below sea level?

Choose one answer:

Lake Assal, Djibouti

Death Valley, USA

Caspian Sea, Central Asia

Sea of Galilee, Israel

Answer: The lake that is the deepest below sea level is the Sea of Galilee, Israel, with a depth of -214 m.

MCQ 111: The recorded temperatures in a particular week were:

$$-2.5^{\circ}\text{C}, 1.2^{\circ}\text{C}, -0.8^{\circ}\text{C}, 0.5^{\circ}\text{C}, -3.2^{\circ}\text{C}$$

Order these temperatures from coldest to warmest.

Choose one answer:

$1.2^{\circ}\text{C} < 0.5^{\circ}\text{C} < -0.8^{\circ}\text{C} < -2.5^{\circ}\text{C}$

$-3.2^{\circ}\text{C} < -2.5^{\circ}\text{C} < -0.8^{\circ}\text{C} < 0.5^{\circ}\text{C} < 1.2^{\circ}\text{C}$

$1.2^{\circ}\text{C} > 0.5^{\circ}\text{C} > -0.8^{\circ}\text{C} > -3.2^{\circ}\text{C}$

$-0.8^{\circ}\text{C} < -2.5^{\circ}\text{C} < -3.2^{\circ}\text{C} < 0.5^{\circ}\text{C} < 1.2^{\circ}\text{C}$

Answer:

- From coldest to warmest: $-3.2^{\circ}\text{C} < -2.5^{\circ}\text{C} < -0.8^{\circ}\text{C} < 0.5^{\circ}\text{C} < 1.2^{\circ}\text{C}$

MCQ 112: Given the years of significant events in Ancient Roman history:

Event	Year
Founding of Rome	-753
End of the Roman Republic	-27
Sacking of Rome by the Gauls	-390
Julius Caesar's assassination	-44

Which event happened the earliest?

Choose one answer:

Founding of Rome

End of the Roman Republic

Sacking of Rome by the Gauls

Julius Caesar's assassination

Answer: The event that happened the earliest was the Founding of Rome in -753 .