

# FRACTIONS

## A DEFINITIONS

**Discover:** Hugo is very hungry after playing soccer. His dad baked two identical cakes. Hugo eats one whole cake:



Then, Hugo is still hungry, so he eats half of the second cake:



How much cake does Hugo eat in total? Write your answer as a fraction.

*Answer:*

- Hugo eats one whole cake and half of another cake.



- The numerator (top number) shows how many parts Hugo eats: 3.
- The denominator (bottom number) shows how many equal parts make one cake: 2.
- So Hugo eats  $\frac{3}{2}$  cakes in total.

### Definition Fraction

A **fraction** includes two numbers: the **numerator** and the **denominator**, separated by a bar.



$$= \frac{3}{2}$$

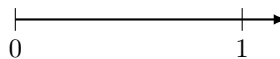
← **numerator:** number of equal parts considered

← **denominator:** number of equal parts the unit is divided

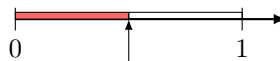
## B ON THE NUMBER LINE

**Discover:**

- Hugo is walking along a path.



- He stops and asks himself, "Where am I?"



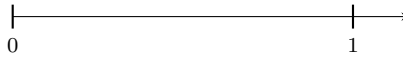
- His father says, "You are at half of the way that is  $\frac{1}{2}$ ."



## Method Representing a Fraction on the Number Line

To represent the fraction  $\frac{2}{3}$  on a number line.

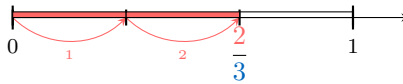
1. Draw a straight line and mark the points 0 and 1.



2. Divide the line between 0 and 1 into 3 equal parts.



3. Count 2 parts from 0 and mark the point.



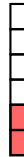
## C EQUIVALENT FRACTIONS

**Discover:** Mr. Tariel has a cake that he cuts into **3 equal parts**. He plans to give **1 part** to his son, Louis.



Louis says, "I want **2 pieces!**"

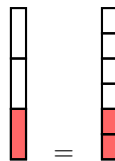
His dad replies, "Alright," and cuts each of the **3 parts** in half, making **6 smaller equal parts**. He then gives Louis **2 of these smaller pieces**.



Louis looks at his plate and feels disappointed.

Why is Louis still not happy?

*Answer:* Even though Louis got **2 pieces** instead of 1, the total amount of cake he received is the same as before. His dad just cut the cake into smaller pieces.

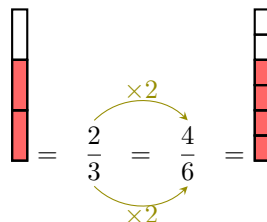


In fractions:



$$\frac{1}{3} = \frac{2}{6}$$

## Definition Equivalent Fractions

When you multiply the numerator and the denominator by the same number, the fractions are equal.




## D ADDITION AND SUBTRACTION

**Discover:** Hugo eats  $\frac{2}{4}$  of a cake:  and Louis eats  $\frac{1}{4}$  of the same cake:   
Which fraction of the cake have Hugo and Louis eaten together?

*Answer:*

$$\begin{array}{c} \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} + \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} = \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} \\ \frac{2}{4} + \frac{1}{4} = \frac{3}{4} \end{array}$$

So Hugo and Louis eat  $\frac{3}{4}$  of the cake together: 

### Definition Addition of Fractions with Common Denominators

When we **add** fractions with common denominators, we keep the denominator the same and add the numerators:

$$\begin{array}{c} \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} + \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} = \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} \\ \frac{2}{4} + \frac{1}{4} = \frac{3}{4} \end{array}$$

### Definition Subtraction of Fractions with Common Denominators

When we **subtract** fractions with common denominators, we keep the denominator the same and subtract the numerators:

$$\begin{array}{c} \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} - \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} = \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} \\ \frac{3}{4} - \frac{1}{4} = \frac{2}{4} \end{array}$$