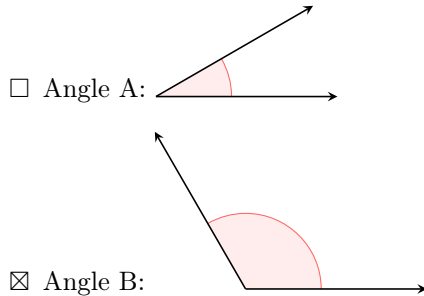


ANGLES

A WHAT IS AN ANGLE?

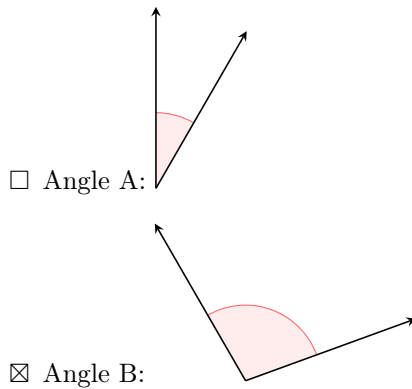
A.1 COMPARING ANGLES

MCQ 1: Which angle has the greater measure?



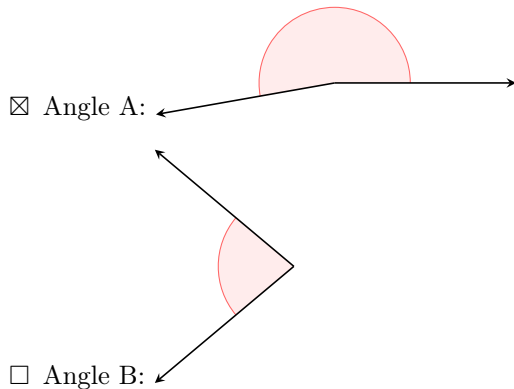
Answer: The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle B has a wider opening (120°) compared to Angle A (30°). Therefore, Angle B is greater.

MCQ 2: Which angle has the greater measure?



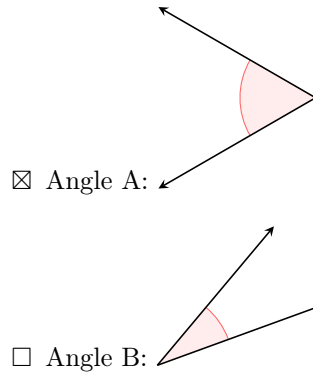
Answer: The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle B has a wider opening (100°) compared to Angle A (30°). Therefore, Angle B is greater.

MCQ 3: Which angle has the greater measure?



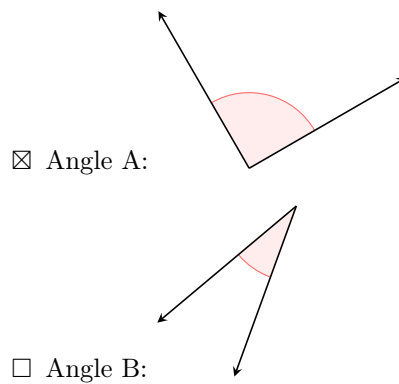
Answer: The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle A has a wider opening (170°) compared to Angle B (80°). Therefore, Angle A is greater.

MCQ 4: Which angle has the greater measure?



Answer: The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle A has a wider opening (60°) compared to Angle B (30°). Therefore, Angle A is greater.

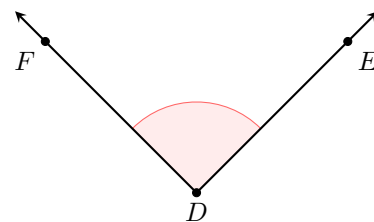
MCQ 5: Which angle has the greater measure?



Answer: The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle A has a wider opening (90°) compared to Angle B (30°). Therefore, Angle A is greater.

A.2 NAMING ANGLES WITH THREE POINTS

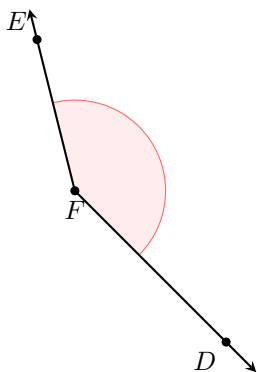
MCQ 6: Which option correctly names the marked angle using three-point notation?



- ☐ $\angle DEF$
- ☒ $\angle FDE$
- ☐ $\angle DFE$

Answer: The marked angle has vertex D , with points E and F on its sides. In three-point notation, the vertex is in the middle, so the correct name is $\angle FDE$.

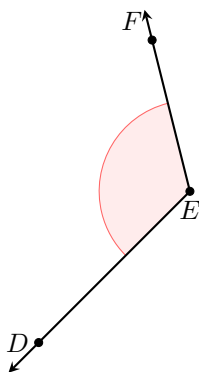
MCQ 7: Which option correctly names the marked angle using three-point notation?



- ☐ $\angle DEF$
☐ $\angle FDE$
☒ $\angle DFE$

Answer: The marked angle has vertex F , with points D and E on its sides. In three-point notation, the vertex is in the middle, so the correct name is $\angle DFE$.

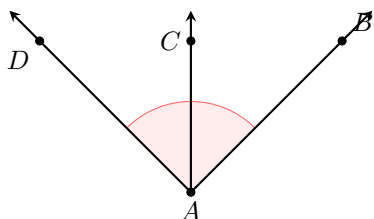
MCQ 8: Which option correctly names the marked angle using three-point notation?



- ☒ $\angle DEF$
☐ $\angle FDE$
☐ $\angle DFE$

Answer: The marked angle has vertex E , with points D and F on its sides. In three-point notation, the vertex is in the middle, so the correct name is $\angle DEF$.

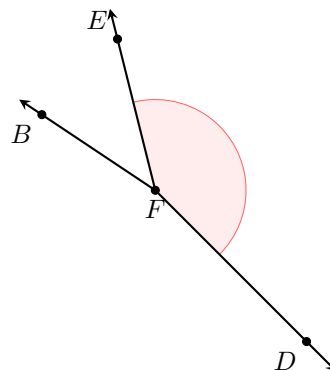
MCQ 9: Which option correctly names the marked angle using three-point notation?



- ☐ $\angle ADC$
☐ $\angle CAB$
☒ $\angle DAB$
☐ $\angle DAC$

Answer: The marked angle has vertex A , with points D and B on its sides. In three-point notation, the vertex is in the middle, so the correct name is $\angle DAB$.

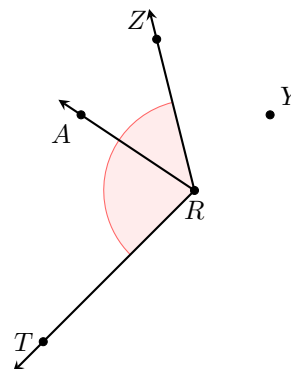
MCQ 10: Which option correctly names the marked angle using three-point notation?



- ☐ $\angle BFD$
☐ $\angle FDE$
☒ $\angle DFE$
☐ $\angle BFE$

Answer: The marked angle has vertex F , with points D and E on its sides. In three-point notation, the vertex is in the middle, so the correct name is $\angle DFE$.

MCQ 11: Which option correctly names the marked angle using three-point notation?



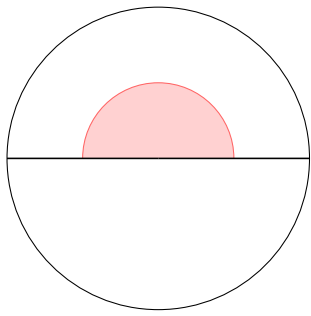
- ☐ $\angle TRY$
☒ $\angle ZRT$
☐ $\angle ZRA$
☐ $\angle RZT$

Answer: The marked angle has vertex R , with points T and Z on its sides. In three-point notation, the vertex is in the middle, so the correct name is $\angle ZRT$.

B DEGREES

B.1 DIVIDING THE FULL TURN

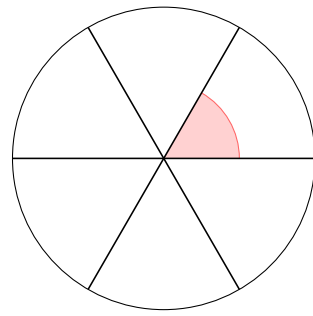
Ex 12:



One-half of a full turn measures $\boxed{180}^\circ$.

Answer:

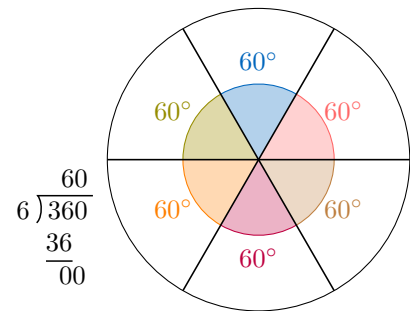
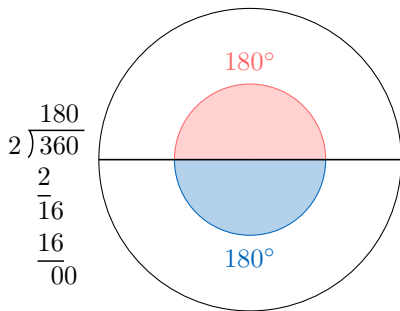
$$\begin{aligned}\text{One-half of a full turn} &= \frac{1}{2} \times 360^\circ \\ &= 360^\circ \div 2 \\ &= 180^\circ\end{aligned}$$




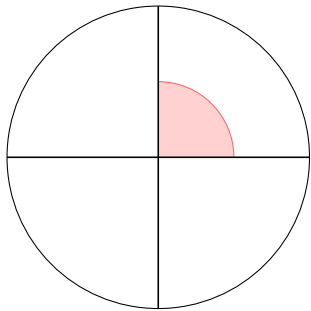
One-sixth of a full turn measures $\boxed{60}^\circ$.

Answer:

$$\begin{aligned}\text{One-sixth of a full turn} &= \frac{1}{6} \times 360^\circ \\ &= 360^\circ \div 6 \\ &= 60^\circ\end{aligned}$$




Ex 13: 

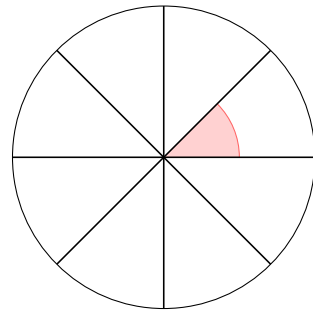


One-quarter of a full turn measures $\boxed{90}^\circ$.

Answer:

$$\begin{aligned}\text{One-quarter of a full turn} &= \frac{1}{4} \times 360^\circ \\ &= 360^\circ \div 4 \\ &= 90^\circ\end{aligned}$$

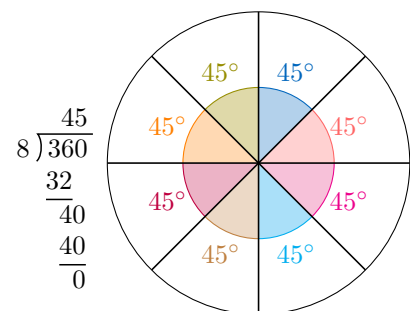
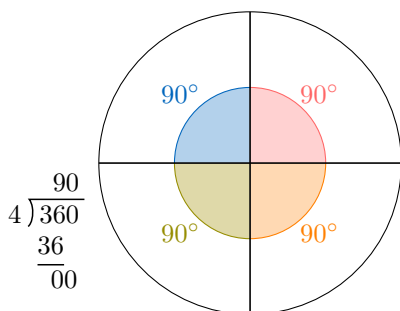
Ex 15: 





One-eighth of a full turn measures $\boxed{45}^\circ$.

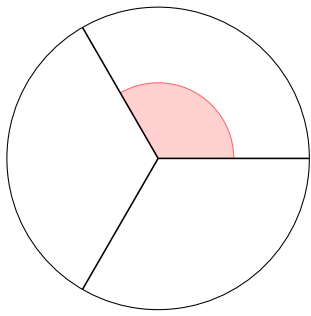
Answer:

$$\begin{aligned}\text{One-eighth of a full turn} &= \frac{1}{8} \times 360^\circ \\ &= 360^\circ \div 8 \\ &= 45^\circ\end{aligned}$$



Ex 14: 

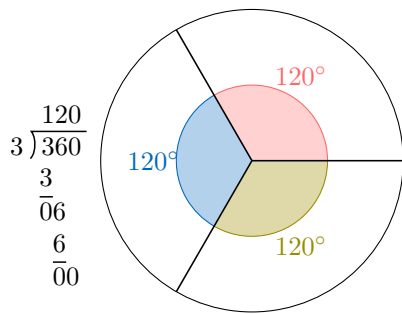
Ex 16: 



One-third of a full turn measures $\boxed{120}^\circ$.

Answer:

$$\begin{aligned}\text{One-third of a full turn} &= \frac{1}{3} \times 360^\circ \\ &= 360^\circ \div 3 \\ &= 120^\circ\end{aligned}$$

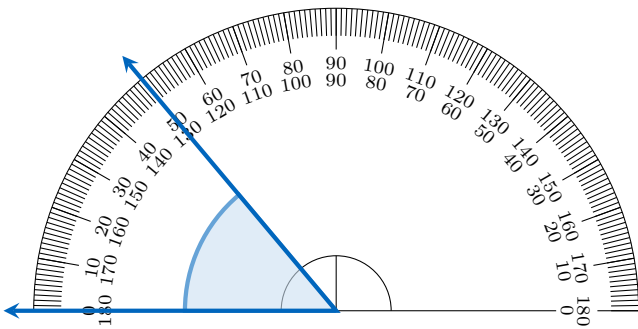


$$\begin{array}{r} 120 \\ 3 \overline{)360} \\ \underline{3} \\ 06 \\ \underline{6} \\ 00 \end{array}$$

C MEASURING AND DRAWING ANGLES WITH A PROTRACTOR

C.1 MEASURING ANGLES

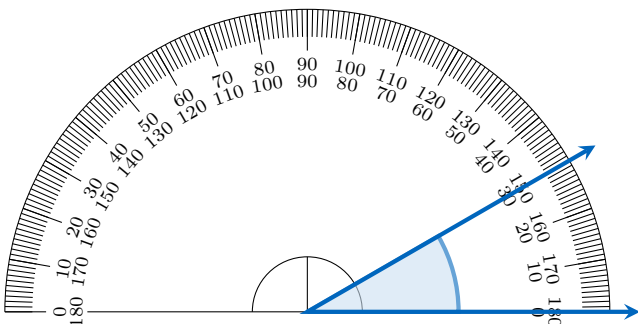
Ex 17:



The angle shown measures $\boxed{50}^\circ$.

Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0° , and the other points to 50° , so the angle measures 50° .

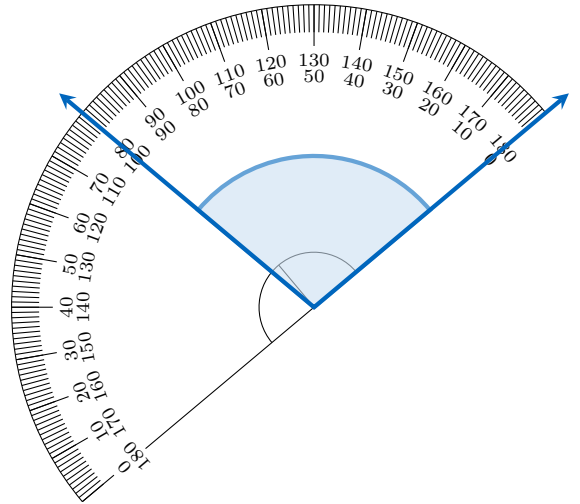
Ex 18:



The angle shown measures $\boxed{30}^\circ$.

Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0° , and the other points to 30° , so the angle measures 30° .

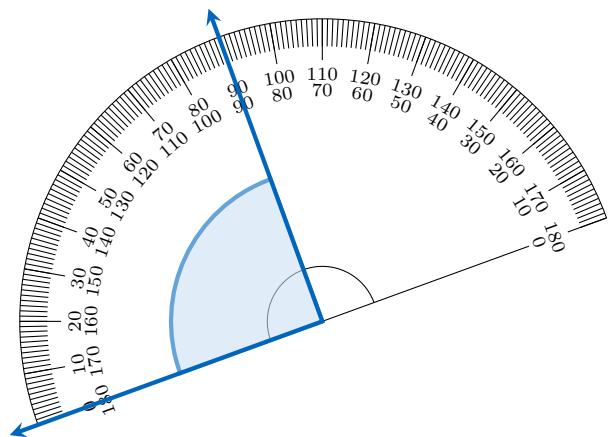
Ex 19:



The angle shown measures $\boxed{100}^\circ$.

Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0° , and the other points to 100° , so the angle measures 100° .

Ex 20:



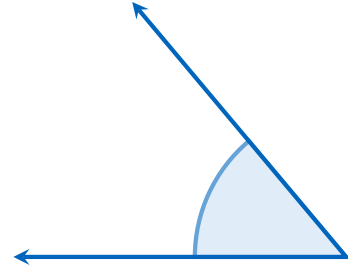
The angle shown measures $\boxed{90}^\circ$.

Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0° , and the other points to 90° , so the angle measures 90° .

Ex 21:

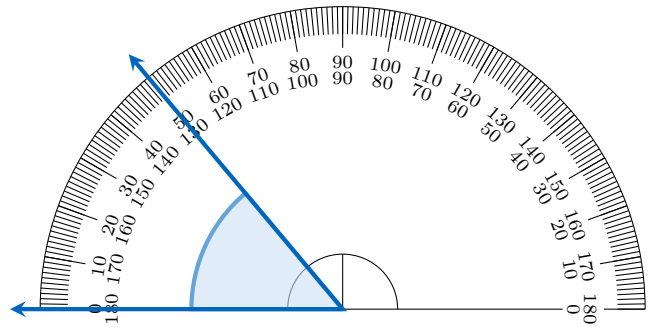
C.2 MEASURING ANGLES

MCQ 24: Using a protractor, find the measure of the angle shown.



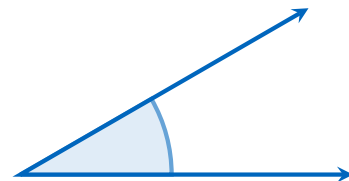
- ☐ 30°
☒ 50°
☐ 90°
☐ 130°

Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale.



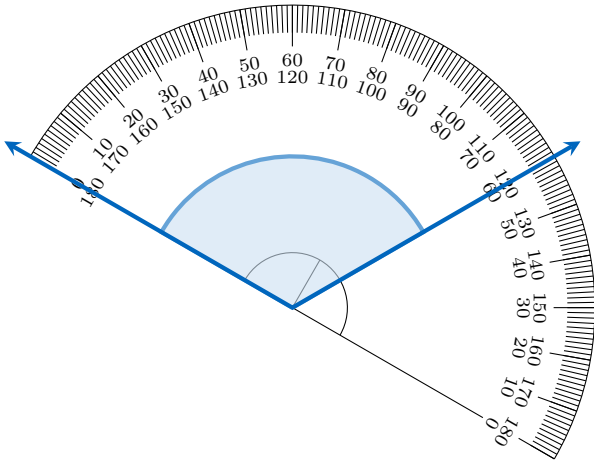
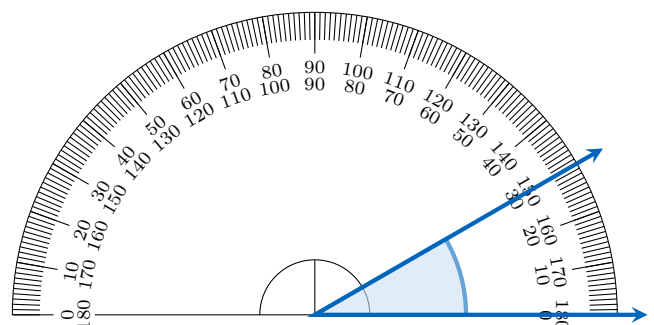
Here, one ray aligns with 0° , and the other points to 50° , so the angle measures 50° .

MCQ 25: Using a protractor, find the measure of the angle shown.



- ☒ 30°
☐ 50°
☐ 90°
☐ 130°

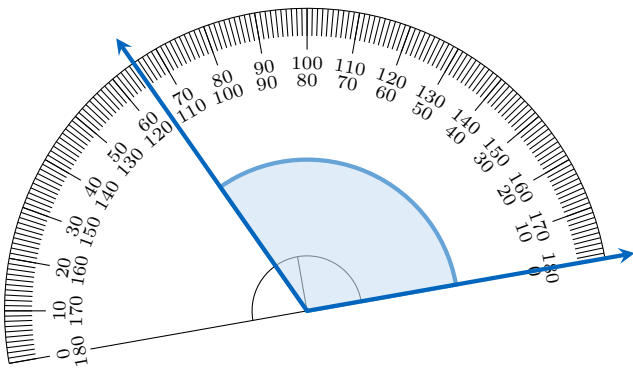
Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale.



The angle shown measures 120° .

Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0° , and the other points to 120° , so the angle measures 120° .

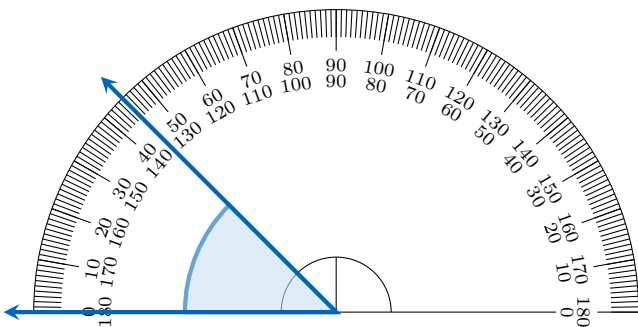
Ex 22:



The angle shown measures 115° .

Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0° , and the other points to 115° , so the angle measures 115° .

Ex 23:



The angle shown measures 45° .

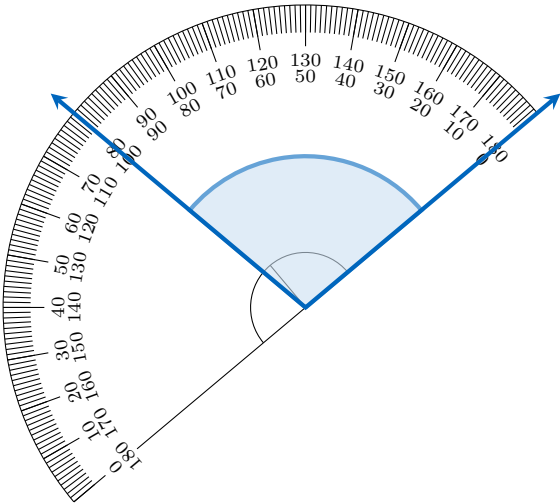
Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0° , and the other points to 45° , so the angle measures 45° .

Here, one ray aligns with 0° , and the other points to 30° , so the angle measures 30° .

MCQ 26: Using a protractor, find the measure of the angle shown.

- ☐ 30°
- ☐ 50°
- ☒ 100°
- ☐ 130°

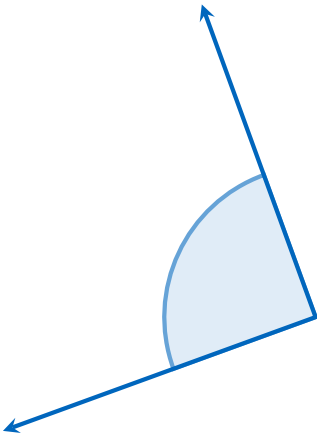
Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale.



Here, one ray aligns with 0° , and the other points to 100° , so the angle measures 100° .

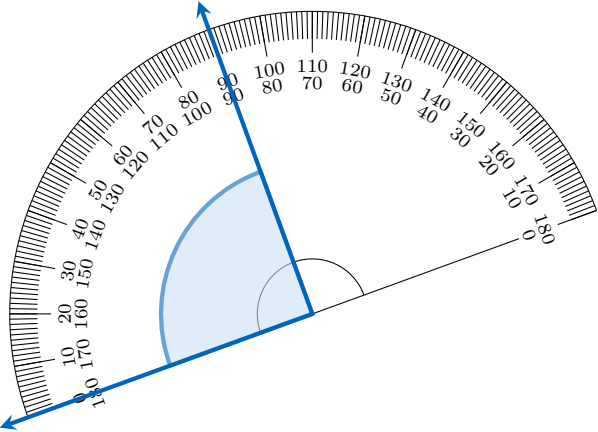
MCQ 27: Using a protractor, find the measure of the angle shown.

- ☐ 30°
- ☐ 50°
- ☒ 90°



☐ 130°

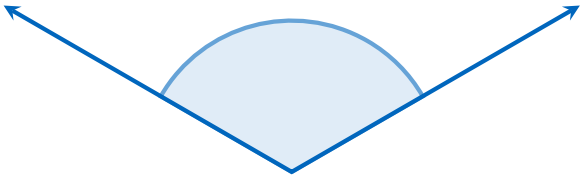
Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale.



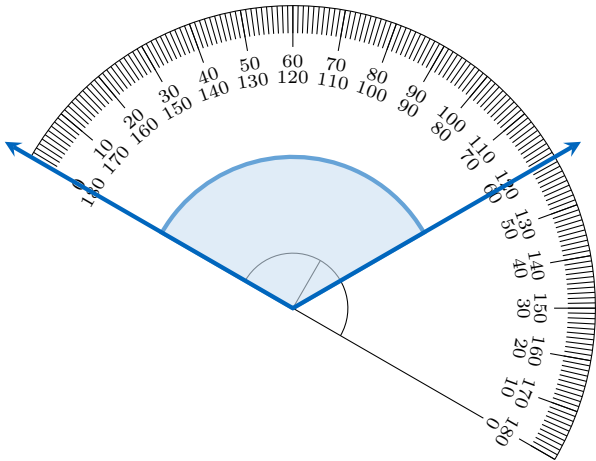
Here, one ray aligns with 0° , and the other points to 90° , so the angle measures 90° .

MCQ 28: Using a protractor, find the measure of the angle shown.

- ☐ 30°
- ☐ 50°
- ☐ 90°
- ☒ 120°



Answer: To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale.



Here, one ray aligns with 0° , and the other points to 120° , so the angle measures 120° .



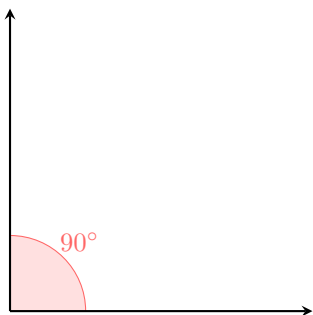
C.3 CONSTRUCTING ANGLES

Ex 29: Using a pencil, a ruler, and a protractor, draw an angle that measures 90° .

Answer: To draw a 90° angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at 0° .
3. Mark a point at 90° on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle measures 90° , as shown below.

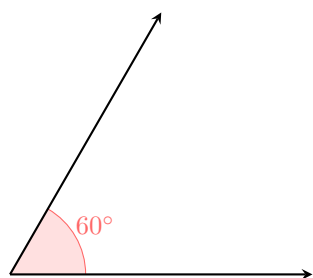


Ex 30: Using a pencil, a ruler, and a protractor, draw an angle that measures 60° .

Answer: To draw a 60° angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at 0° .
3. Mark a point at 60° on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle measures 60° , as shown below.

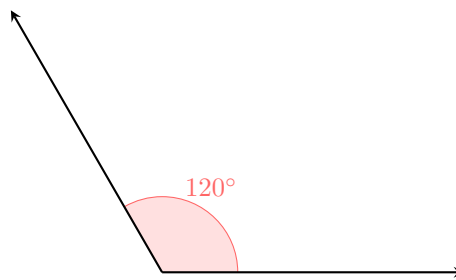


Ex 31: Using a pencil, a ruler, and a protractor, draw an angle that measures 120° .

Answer: To draw a 120° angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at 0° .
3. Mark a point at 120° on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle measures 120° , as shown below.

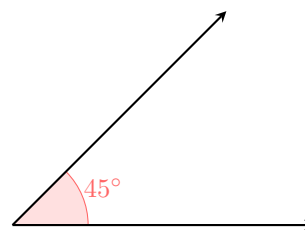


Ex 32: Using a pencil, a ruler, and a protractor, draw an angle that measures 45° .

Answer: To draw a 45° angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at 0° .
3. Mark a point at 45° on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

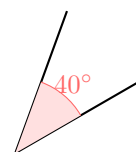
The resulting angle measures 45° , as shown below.



D CLASSIFICATION OF ANGLES

D.1 IDENTIFYING ANGLE TYPES BY MEASURE

MCQ 33: What is the nature of the marked angle?



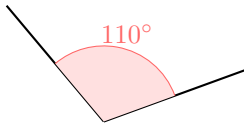
Choose one answer:

- ☒ Acute angle
- ☐ Right angle
- ☐ Obtuse angle
- ☐ Straight angle

Answer:

- An acute angle measures less than 90 degrees.
- The marked angle, measuring 40° , is acute because it is less than 90° .

MCQ 34: What is the nature of the marked angle?



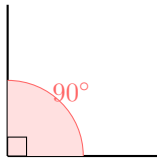
Choose one answer:

- ☐ Acute angle
- ☐ Right angle
- ☒ Obtuse angle
- ☐ Straight angle

Answer:

- An obtuse angle measures more than 90 degrees but less than 180 degrees.
- The marked angle, measuring 110° , is obtuse because it is between 90° and 180° .

MCQ 35: What is the nature of the marked angle?



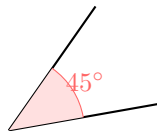
Choose one answer:

- ☐ Acute angle
- ☒ Right angle
- ☐ Obtuse angle
- ☐ Straight angle

Answer:

- A right angle measures exactly 90 degrees.
- The marked angle, measuring 90° , is a right angle.

MCQ 36: What is the nature of the marked angle?



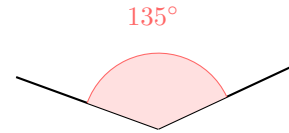
Choose one answer:

- ☒ Acute angle
- ☐ Right angle
- ☐ Obtuse angle
- ☐ Straight angle

Answer:

- An acute angle measures less than 90 degrees.
- The marked angle, measuring 45° , is acute because it is less than 90° .

MCQ 37: What is the nature of the marked angle?



Choose one answer:

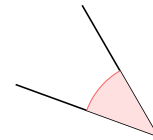
- ☐ Acute angle
- ☐ Right angle
- ☒ Obtuse angle
- ☐ Straight angle

Answer:

- An obtuse angle measures more than 90 degrees but less than 180 degrees.
- The marked angle, measuring 135° , is obtuse because it is between 90° and 180° .

D.2 IDENTIFYING ANGLE TYPES

MCQ 38: Identify the type of the highlighted angle.

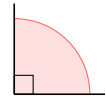


Choose one answer:

- ☒ acute angle
- ☐ right angle
- ☐ obtuse angle
- ☐ straight angle

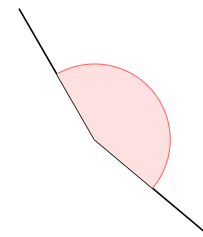
Answer:

- An acute angle measures less than 90° .
- The highlighted angle ($\approx 40^\circ$) is less open than a right angle



- Hence it is **acute**.

MCQ 39: Identify the type of the highlighted angle.





Choose one answer:

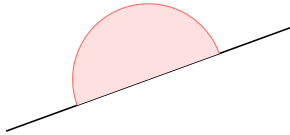
- ☐ acute angle
- ☐ right angle

- ☒ obtuse angle
- ☐ straight angle

Answer:

- An obtuse angle measures between 90° and 180° .
- The highlighted angle ($\approx 160^\circ$) is more open than a right angle  but less than a straight angle .
- Therefore it is **obtuse**.

MCQ 40: Identify the type of the highlighted angle.



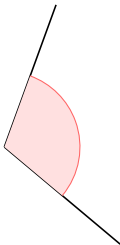
Choose one answer:

- ☐ acute angle
- ☐ right angle
- ☐ obtuse angle
- ☒ straight angle

Answer:

- A straight angle measures exactly 180° .
- The highlighted angle forms a line.
- It is therefore **straight**.

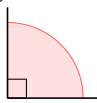

MCQ 41: Identify the type of the highlighted angle.



Choose one answer:

- ☐ acute angle
- ☐ right angle
- ☒ obtuse angle
- ☐ straight angle

Answer:

- An obtuse angle measures between 90° and 180° .
- The highlighted angle ($\approx 110^\circ$) is more open than a right angle  but less open than a straight angle .
- Therefore it is **obtuse**.

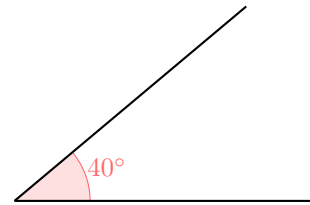
D.3 CONSTRUCTING ANGLE TYPES

Ex 42: Using a pencil, a ruler, and a protractor, draw an acute angle.

Answer: To draw an acute angle, such as a 40° angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at 0° .
3. Mark a point at 40° on the protractor's scale (any angle less than 90° is acceptable).
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle is acute, measuring less than 90° , as shown below.

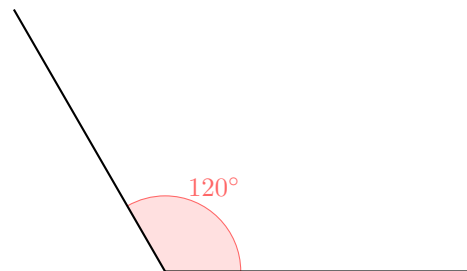


Ex 43: Using a pencil, a ruler, and a protractor, draw an obtuse angle.

Answer: To draw an obtuse angle, such as a 120° angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at 0° .
3. Mark a point at 120° on the protractor's scale (any angle greater than 90° but less than 180° is acceptable).
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle is obtuse, measuring greater than 90° but less than 180° , as shown below.

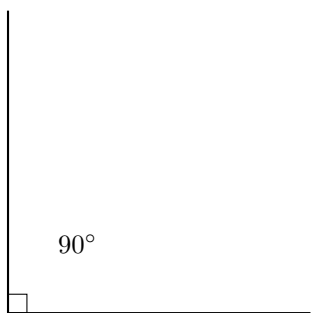


Ex 44: Using a pencil, a ruler, and a protractor, draw a right angle.

Answer: To draw a right angle, which measures 90° :

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at 0° .
3. Mark a point at 90° on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

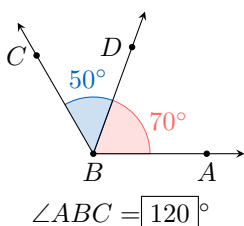
The resulting angle is a right angle, measuring exactly 90° , as shown below.



E ANGLE ADDITION

E.1 ADDING ANGLES

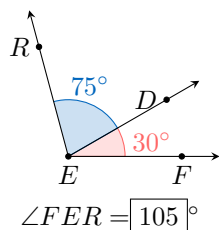
Ex 45: Calculate the measure of $\angle ABC$.



Answer: Using the angle addition postulate, $\angle ABC$ is the sum of the smaller angles $\angle ABD$ and $\angle DBC$:

$$\begin{aligned}\angle ABC &= \angle ABD + \angle DBC \\ &= 70^\circ + 50^\circ \\ &= 120^\circ\end{aligned}$$

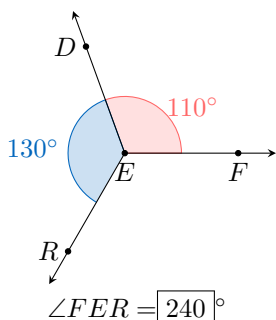
Ex 46: Calculate the measure of $\angle FER$.



Answer: Using the angle addition postulate, $\angle FER$ is the sum of the smaller angles $\angle FED$ and $\angle DER$:

$$\begin{aligned}\angle FER &= \angle FED + \angle DER \\ &= 30^\circ + 75^\circ \\ &= 105^\circ\end{aligned}$$

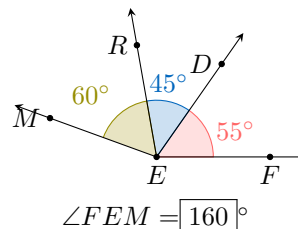
Ex 47: Calculate the measure of $\angle FER$.



Answer: Using the angle addition postulate, $\angle FER$ is the sum of the smaller angles $\angle FED$ and $\angle DER$:

$$\begin{aligned}\angle FER &= \angle FED + \angle DER \\ &= 110^\circ + 130^\circ \\ &= 240^\circ\end{aligned}$$

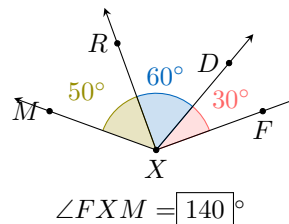
Ex 48: Calculate the measure of $\angle FEM$.



Answer: Using the angle addition postulate, $\angle FEM$ is the sum of the smaller angles $\angle FED$, $\angle DER$, and $\angle REM$:

$$\begin{aligned}\angle FEM &= \angle FED + \angle DER + \angle REM \\ &= 55^\circ + 45^\circ + 60^\circ \\ &= 160^\circ\end{aligned}$$

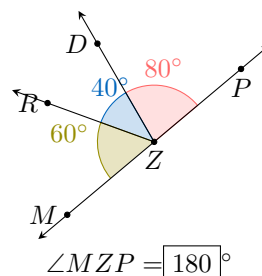
Ex 49: Calculate the measure of $\angle FXM$.



Answer: Using the angle addition postulate, $\angle FXM$ is the sum of the smaller angles $\angle FXD$, $\angle DXR$, and $\angle RXM$:

$$\begin{aligned}\angle FXM &= \angle FXD + \angle DXR + \angle RXM \\ &= 30^\circ + 60^\circ + 50^\circ \\ &= 140^\circ\end{aligned}$$

Ex 50: Calculate the measure of $\angle MZP$.

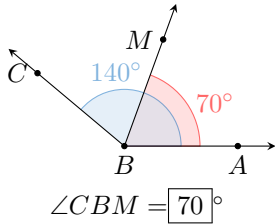


Answer: Using the angle addition postulate, $\angle MZP$ is the sum of the smaller angles $\angle MZR$, $\angle RZD$, and $\angle DZP$:

$$\begin{aligned}\angle MZP &= \angle MZR + \angle RZD + \angle DZP \\ &= 60^\circ + 40^\circ + 80^\circ \\ &= 180^\circ\end{aligned}$$

E.2 SUBTRACTING ANGLES

Ex 51: Calculate the measure of $\angle CBM$.



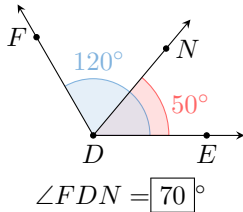
Answer: Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle CBM + \angle MBA = \angle CBA$$

To find $\angle CBM$, subtract $\angle MBA$ from $\angle CBA$:

$$\begin{aligned}\angle CBM &= \angle CBA - \angle MBA \\ &= 140^\circ - 70^\circ \\ &= 70^\circ\end{aligned}$$

Ex 52: Calculate the measure of $\angle FDN$.



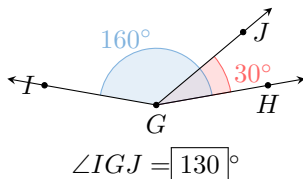
Answer: Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle FDN + \angle NDE = \angle FDE$$

To find $\angle FDN$, subtract $\angle NDE$ from $\angle FDE$:

$$\begin{aligned}\angle FDN &= \angle FDE - \angle NDE \\ &= 120^\circ - 50^\circ \\ &= 70^\circ\end{aligned}$$

Ex 53: Calculate the measure of $\angle IGJ$.



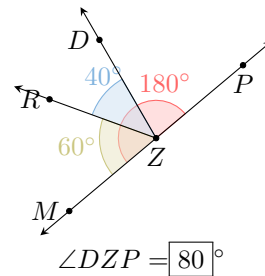
Answer: Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle IGJ + \angle JGH = \angle IGH$$

To find $\angle IGJ$, subtract $\angle JGH$ from $\angle IGH$:

$$\begin{aligned}\angle IGJ &= \angle IGH - \angle JGH \\ &= 160^\circ - 30^\circ \\ &= 130^\circ\end{aligned}$$

Ex 54: Calculate the measure of $\angle DZP$ by subtracting the known angles from the larger angle using the angle addition postulate.



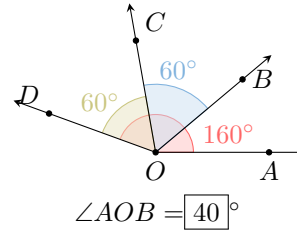
Answer: Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle MZR + \angle RZD + \angle DZP = \angle MZP$$

To find $\angle DZP$, subtract $\angle MZR$ and $\angle RZD$ from $\angle MZP$:

$$\begin{aligned}\angle DZP &= \angle MZP - \angle MZR - \angle RZD \\ &= 180^\circ - 60^\circ - 40^\circ \\ &= 80^\circ\end{aligned}$$

Ex 55: Calculate the measure of $\angle AOB$ by subtracting the known angles from the larger angle using the angle addition postulate.



Answer: Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle AOB + \angle BOC + \angle COD = \angle AOD$$

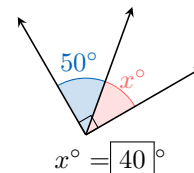
To find $\angle AOB$, subtract $\angle BOC$ and $\angle COD$ from $\angle AOD$:

$$\begin{aligned}\angle AOB &= \angle AOD - \angle BOC - \angle COD \\ &= 160^\circ - 60^\circ - 60^\circ \\ &= 40^\circ\end{aligned}$$

F ANGLE PROPERTIES

F.1 CALCULATING AN UNKNOWN ANGLE IN A RIGHT ANGLE

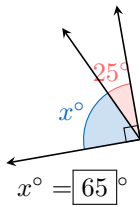
Ex 56: Calculate the measure of the unknown angle.



Answer: The sum of angles in a right angle is equal to 90° .

$$\begin{aligned}x^\circ + 50^\circ &= 90^\circ \\ x^\circ &= 90^\circ - 50^\circ \quad (\text{subtract } 50^\circ) \\ &= 40^\circ\end{aligned}$$

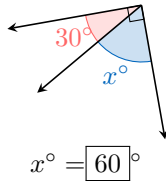
Ex 57: Calculate the measure of the unknown angle.



Answer: The sum of angles in a right angle is equal to 90° .

$$\begin{aligned} 25^\circ + x^\circ &= 90^\circ \\ x^\circ &= 90^\circ - 25^\circ \quad (\text{subtract } 25^\circ) \\ &= 65^\circ \end{aligned}$$

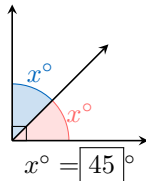
Ex 58: Calculate the measure of the unknown angle.



Answer: The sum of angles in a right angle is equal to 90° .

$$\begin{aligned} 30^\circ + x^\circ &= 90^\circ \\ x^\circ &= 90^\circ - 30^\circ \quad (\text{subtract } 30^\circ) \\ &= 60^\circ \end{aligned}$$

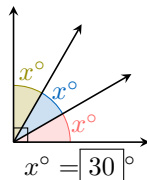
Ex 59: Calculate the measure of the unknown angle.



Answer: The sum of angles in a right angle is equal to 90° . The two angles are equal (x°).

$$\begin{aligned} x^\circ + x^\circ &= 90^\circ \\ 2x^\circ &= 90^\circ \quad (\text{combine like terms}) \\ x^\circ &= 90^\circ \div 2 \quad (\text{divide by 2}) \\ &= 45^\circ \end{aligned}$$

Ex 60: Calculate the measure of the unknown angle.

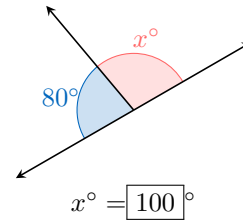


Answer: The sum of angles in a right angle is equal to 90° . The three angles are equal (x°).

$$\begin{aligned} x^\circ + x^\circ + x^\circ &= 90^\circ \\ 3x^\circ &= 90^\circ \quad (\text{combine like terms}) \\ x^\circ &= 90^\circ \div 3 \quad (\text{divide by 3}) \\ &= 30^\circ \end{aligned}$$

F.2 CALCULATING AN UNKNOWN ANGLE IN A STRAIGHT ANGLE

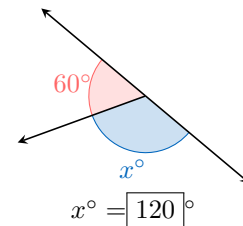
Ex 61: Calculate the measure of the unknown angle.



Answer: The sum of angles on a straight line is equal to 180° .

$$\begin{aligned} x^\circ + 80^\circ &= 180^\circ \\ x^\circ &= 180^\circ - 80^\circ \quad (\text{subtract } 80^\circ) \\ &= 100^\circ \end{aligned}$$

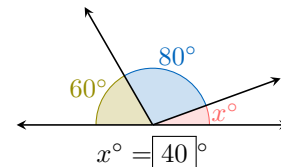
Ex 62: Calculate the measure of the unknown angle.



Answer: The sum of angles on a straight line is equal to 180° .

$$\begin{aligned} 60^\circ + x^\circ &= 180^\circ \\ x^\circ &= 180^\circ - 60^\circ \quad (\text{subtract } 60^\circ) \\ &= 120^\circ \end{aligned}$$

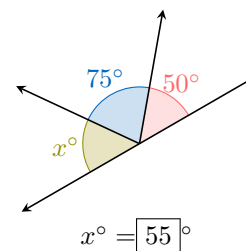
Ex 63: Calculate the measure of the unknown angle.



Answer: The sum of angles on a straight line is equal to 180° .

$$\begin{aligned} x^\circ + 80^\circ + 60^\circ &= 180^\circ \\ x^\circ &= 180^\circ - 80^\circ - 60^\circ \quad (\text{subtract } 80^\circ \text{ and } 60^\circ) \\ &= 40^\circ \end{aligned}$$

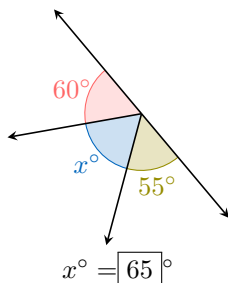
Ex 64: Calculate the measure of the unknown angle.



Answer: The sum of angles on a straight line is equal to 180° .

$$\begin{aligned} 50^\circ + 75^\circ + x^\circ &= 180^\circ \\ x^\circ &= 180^\circ - 50^\circ - 75^\circ \quad (\text{subtract } 50^\circ \text{ and } 75^\circ) \\ &= 55^\circ \end{aligned}$$

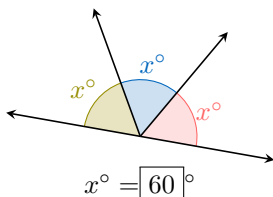
Ex 65: Calculate the measure of the unknown angle.



Answer: The sum of angles on a straight line is equal to 180° .

$$\begin{aligned} 60^\circ + x^\circ + 55^\circ &= 180^\circ \\ x^\circ &= 180^\circ - 60^\circ - 55^\circ \quad (\text{subtract } 60^\circ \text{ and } 55^\circ) \\ &= 65^\circ \end{aligned}$$

Ex 66: Calculate the measure of the unknown angle.

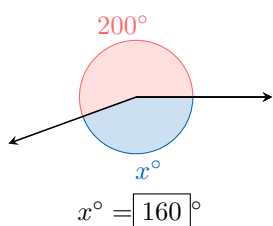


Answer: The sum of angles on a straight line is equal to 180° . The three angles are equal (x°).

$$\begin{aligned} x^\circ + x^\circ + x^\circ &= 180^\circ \\ 3x^\circ &= 180^\circ \quad (\text{combine like terms}) \\ x^\circ &= 180^\circ \div 3 \quad (\text{divide by 3}) \\ &= 60^\circ \end{aligned}$$

F.3 CALCULATING AN UNKNOWN ANGLE IN A FULL ANGLE

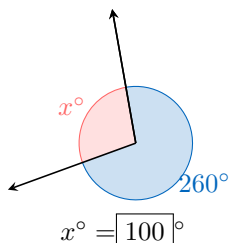
Ex 67: Calculate the measure of the unknown angle.



Answer: The sum of angles in a point is equal to 360° .

$$\begin{aligned} 200^\circ + x^\circ &= 360^\circ \\ x^\circ &= 360^\circ - 200^\circ \quad (\text{subtract } 200^\circ) \\ &= 160^\circ \end{aligned}$$

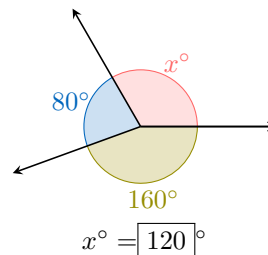
Ex 68: Calculate the measure of the unknown angle.



Answer: The sum of angles around a point is equal to 360° .

$$\begin{aligned} x^\circ + 260^\circ &= 360^\circ \\ x^\circ &= 360^\circ - 260^\circ \quad (\text{subtract } 260^\circ) \\ &= 100^\circ \end{aligned}$$

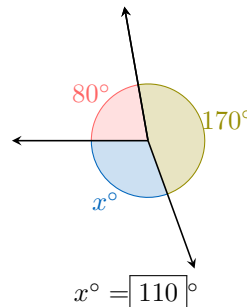
Ex 69: Calculate the measure of the unknown angle.



Answer: The sum of angles around a point is equal to 360° .

$$\begin{aligned} x^\circ + 80^\circ + 160^\circ &= 360^\circ \\ x^\circ &= 360^\circ - 80^\circ - 160^\circ \quad (\text{subtract } 80^\circ \text{ and } 160^\circ) \\ &= 120^\circ \end{aligned}$$

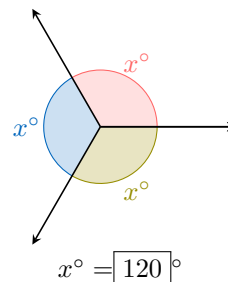
Ex 70: Calculate the measure of the unknown angle.



Answer: The sum of angles around a point is equal to 360° .

$$\begin{aligned} 80^\circ + x^\circ + 170^\circ &= 360^\circ \\ x^\circ &= 360^\circ - 80^\circ - 170^\circ \quad (\text{subtract } 80^\circ \text{ and } 170^\circ) \\ &= 110^\circ \end{aligned}$$

Ex 71: Calculate the measure of the unknown angle.



Answer: The sum of angles around a point is equal to 360° . The three angles are equal (x°).

$$\begin{aligned} x^\circ + x^\circ + x^\circ &= 360^\circ \\ 3x^\circ &= 360^\circ \quad (\text{combine like terms}) \\ x^\circ &= 360^\circ \div 3 \quad (\text{divide by 3}) \\ &= 120^\circ \end{aligned}$$